

The feasibility of dynamic full-field earthquake measurements from space: a laboratory study

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California Institute of Technology



Geostationary Telescope Meeting
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GALCIT

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Acknowledgments:

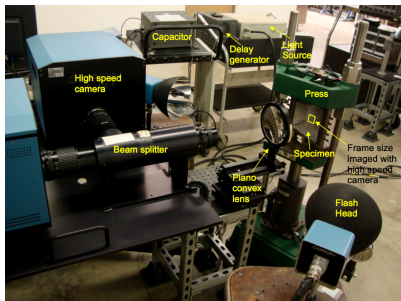
*Sebastien Leprince, Mike Mello,
Laurence Bodelot, Vahe Gabuchian*

Summary

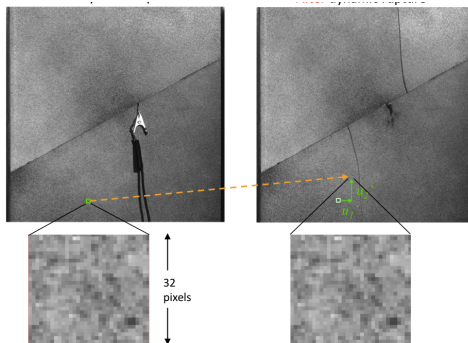
Background



Experimental setup

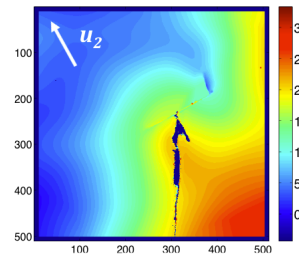
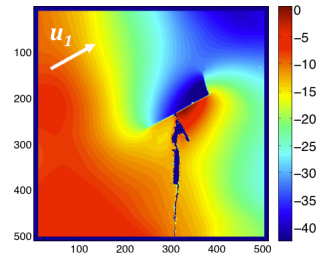


Experimental Method: Digital Image Correlation



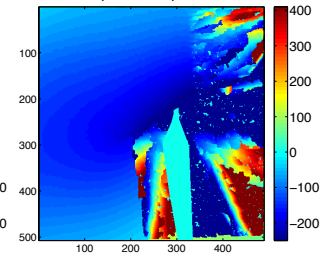
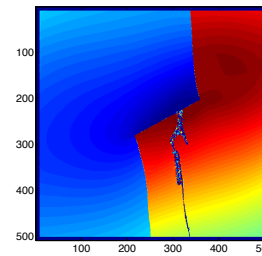
Displacement field – Test1

The importance of filtering data

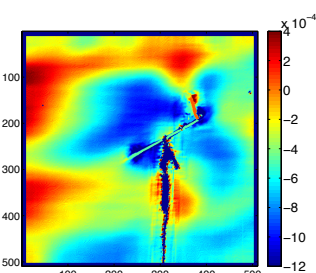
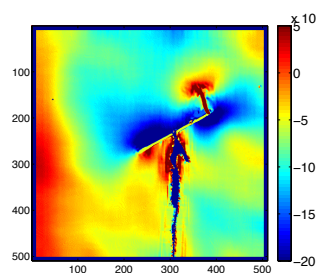


Displacement field – Test2

COSI-Corr vs. VIC-2D

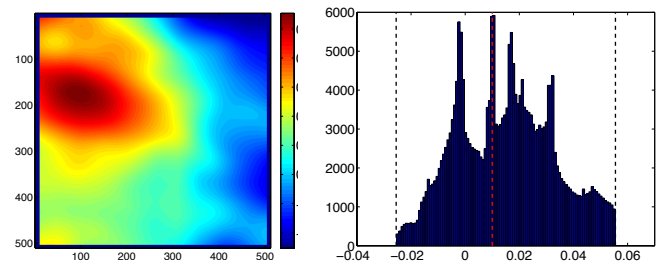


Strains– Test1



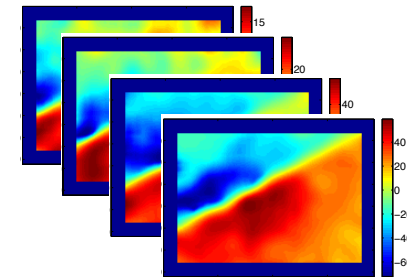
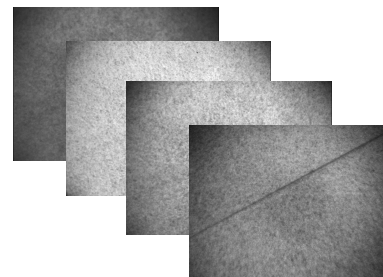
How accurate are our results

Error analysis



High Speed Photography

Preliminary results

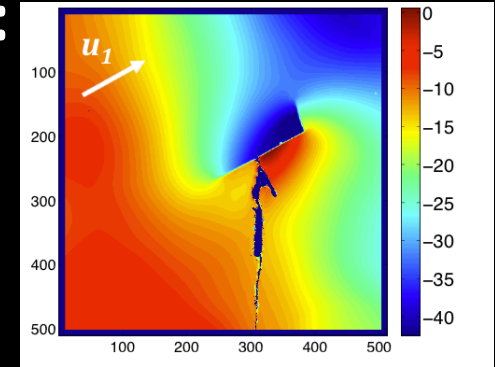
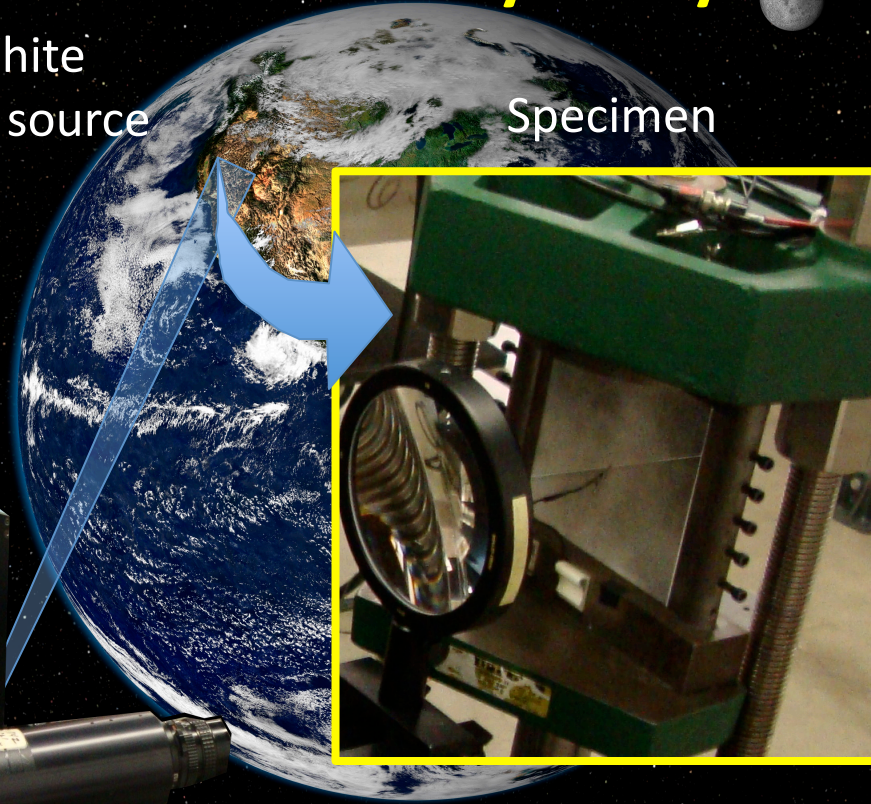
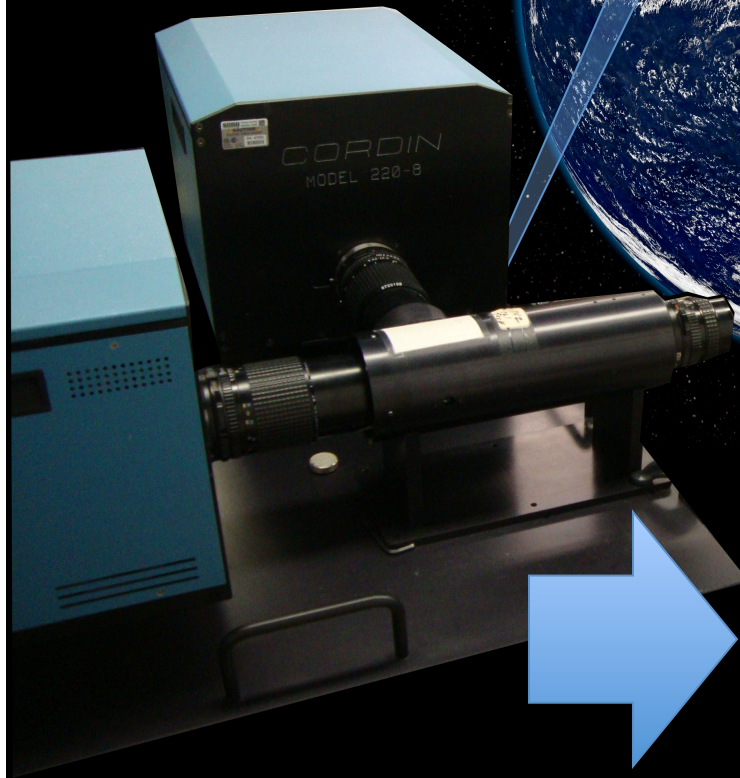


Geostationary Space Telescope: A Laboratory Study

White
Light source

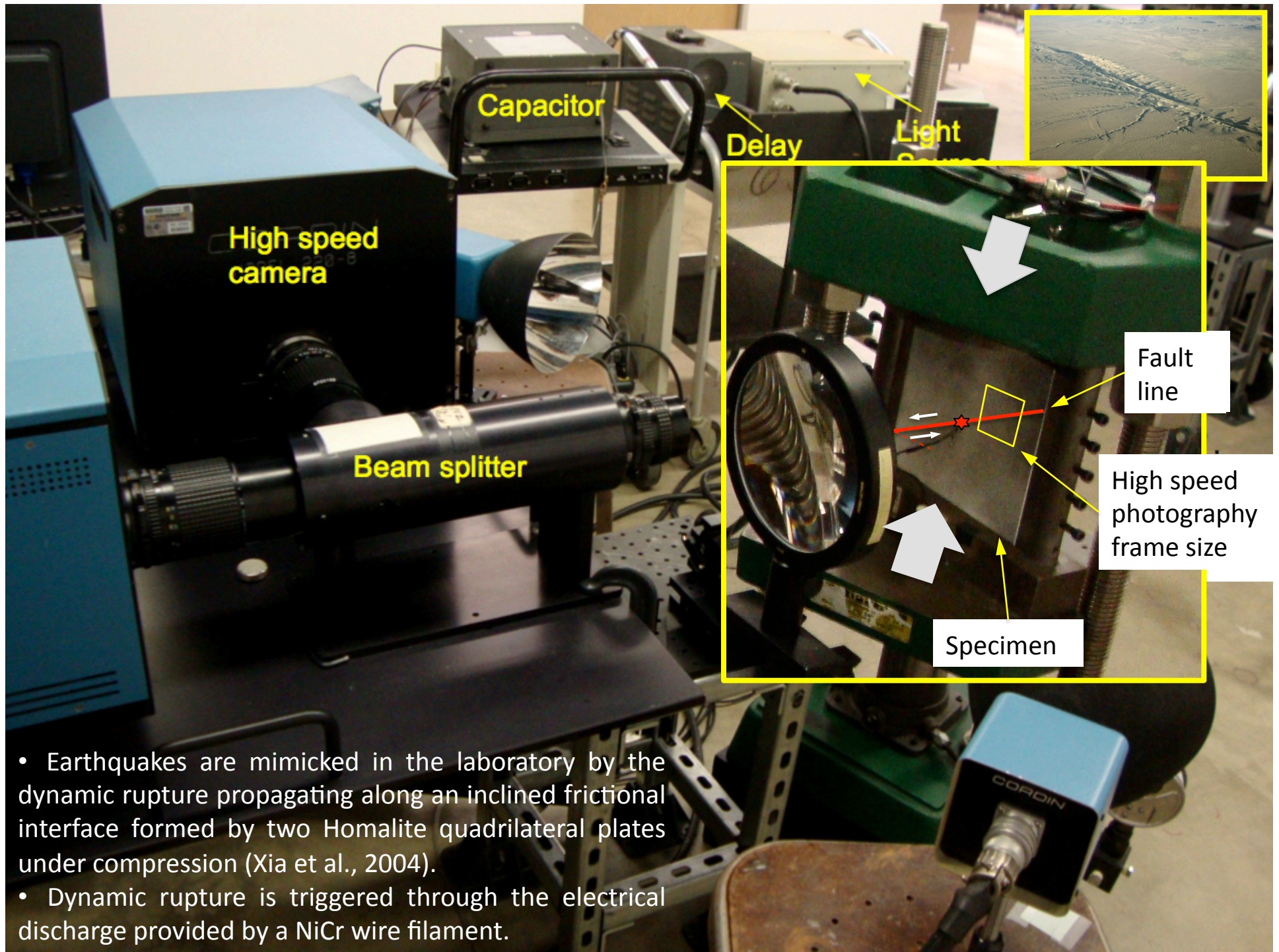
Specimen

High speed
camera system



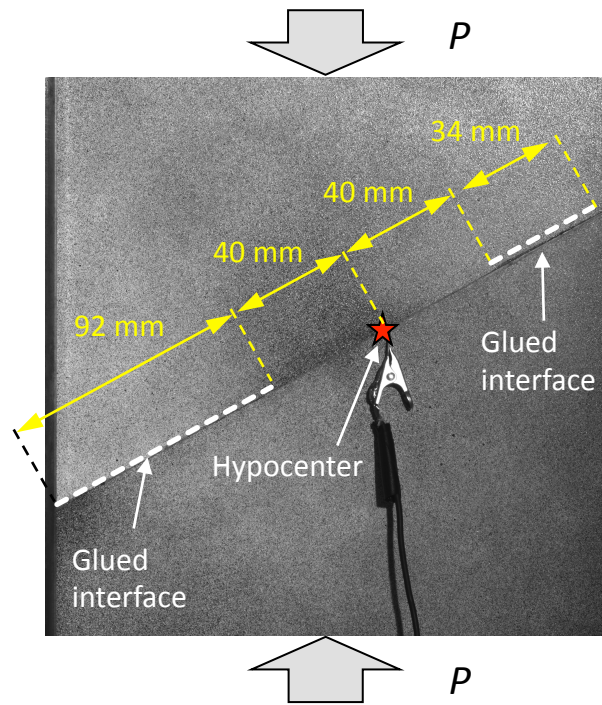
Analyze images
with
Digital Image
Correlation techniques
(e.g. COSI-Corr, VIC-2D)





- Earthquakes are mimicked in the laboratory by the dynamic rupture propagating along an inclined frictional interface formed by two Homalite quadrilateral plates under compression (Xia et al., 2004).
- Dynamic rupture is triggered through the electrical discharge provided by a NiCr wire filament.

Geometry and Loading Configuration



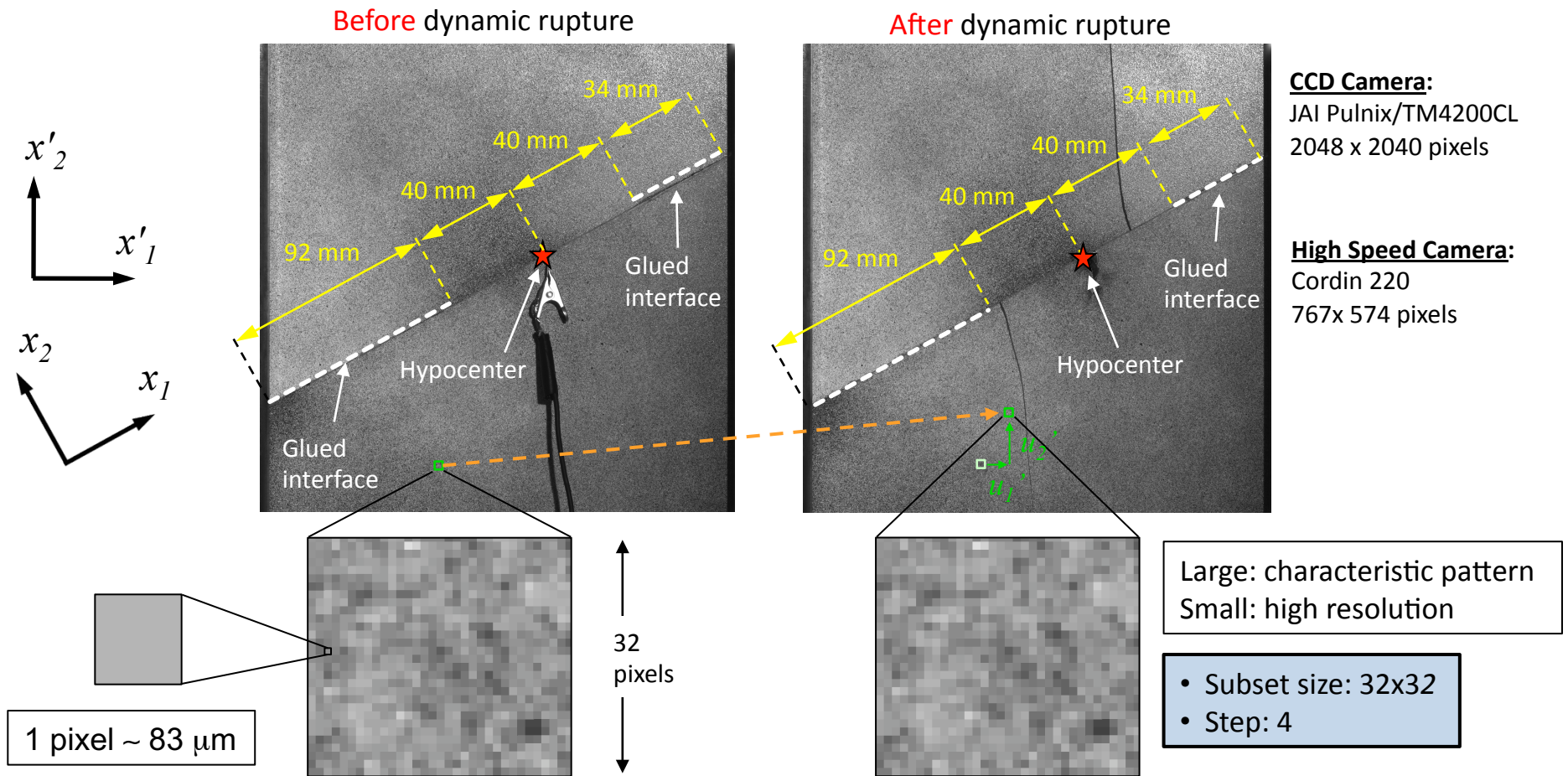
We will discuss two tests:

- $P = 5$ MPa (subRayleigh)
- $P = 15$ MPa (supershear)



Expected
rupture speed
(from previous
experiments)

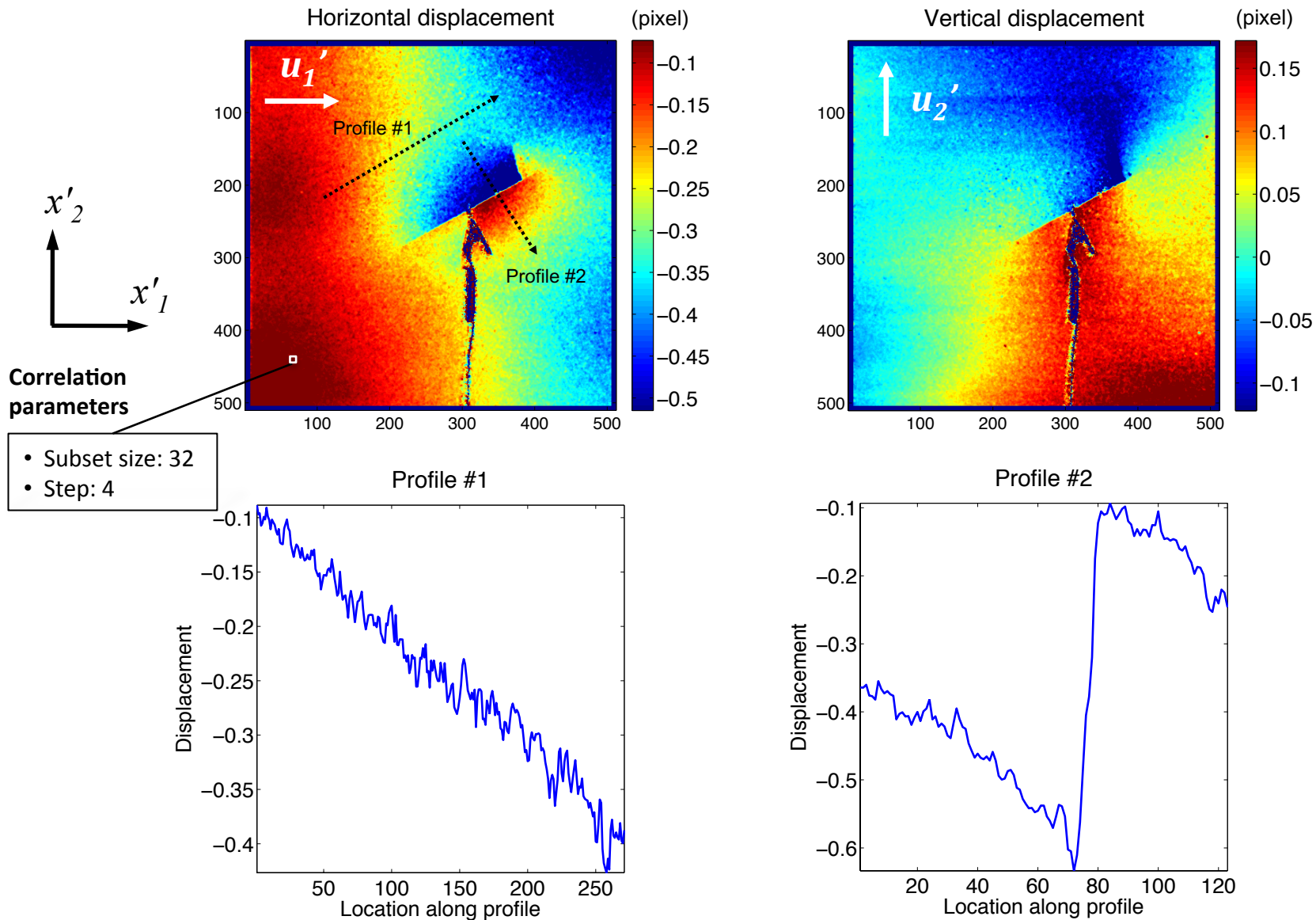
The Digital Image Correlation Method



- Digital Image Correlation (DIC) is an optical method to measure the deformation on a specimen surface.
- DIC technique identifies gray level patterns in small pixel subsets and tracks their motion during deformation.
- Two methods are used in this study:
 - **COSI-Corr** (Leprince et. al, 2007).
 - **VIC-2D** (Correlated Solutions Inc.)

Displacement Field - *Unfiltered*

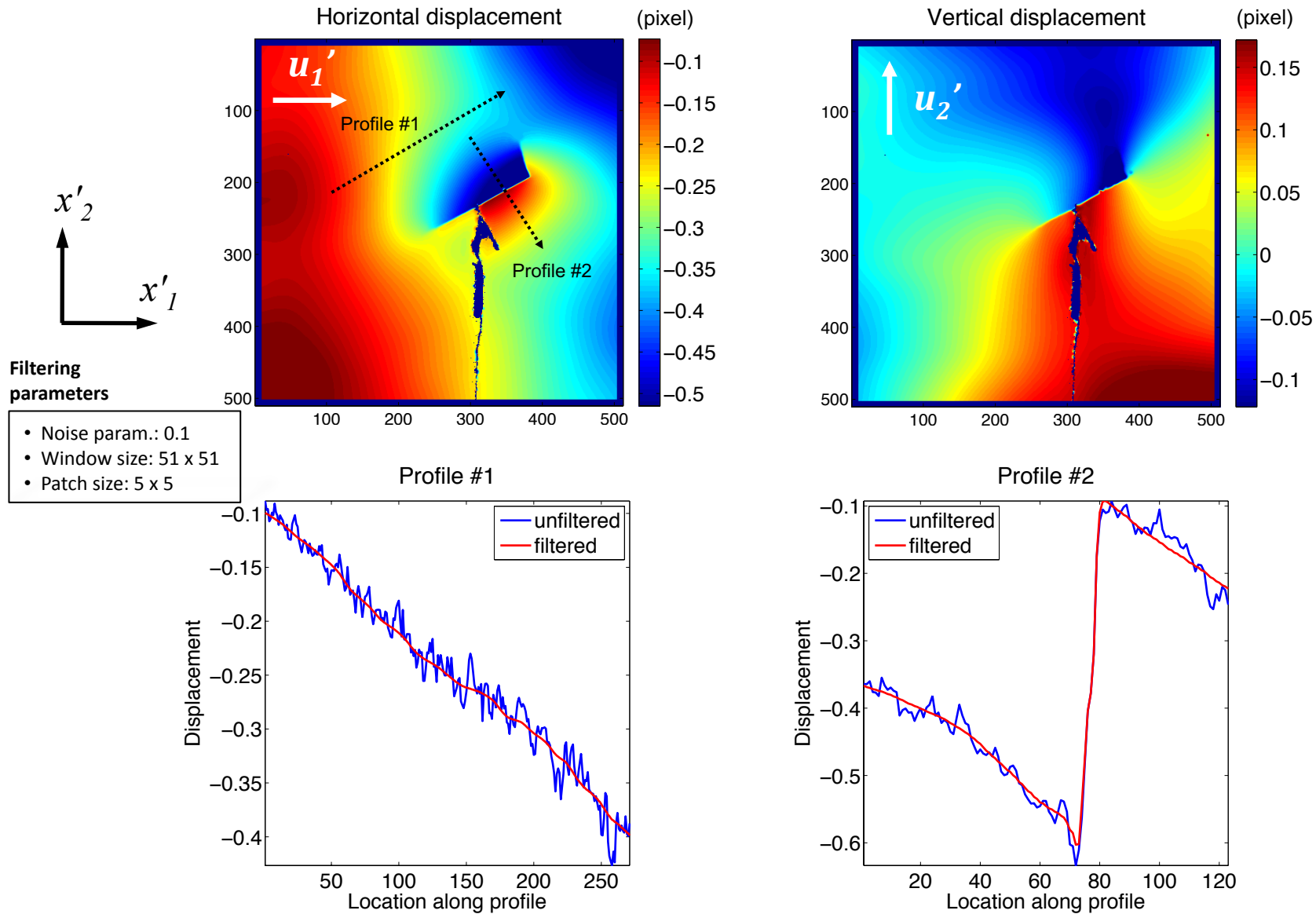
Test 1, $P = 5$ MPa



Displacement Field - *Filtered*

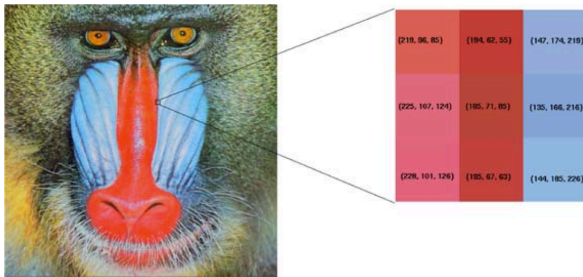
← Non local means filter
(Buades et al., 2008)

Test 1, $P = 5$ MPa

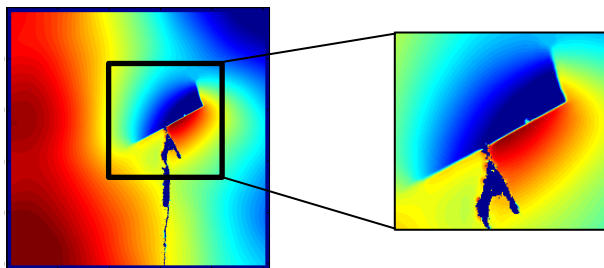
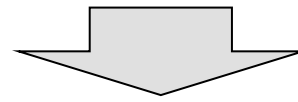


The Non Local Means Filter (NL-Means)

(Buades et al., 2008; Goosens et al. 2008)



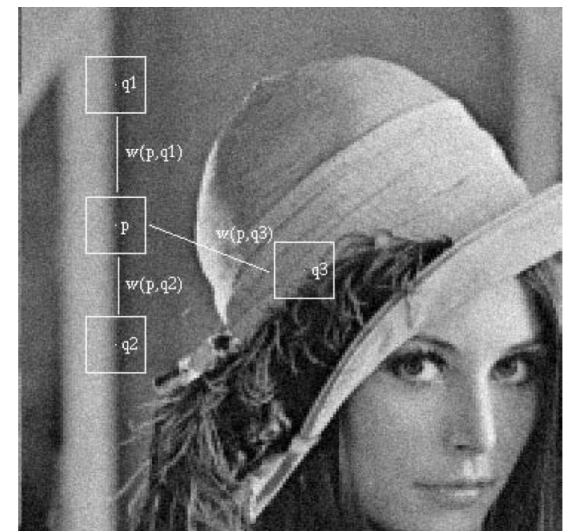
- Local smoothing filters give blurred edges
- In contrast the NL-means filter avoids the blurring effect



- It is very useful to accurately reproduce the displacement field of our experiments, which contains sharp edges near the interface and wing cracks.



- In an image, most details occur repeatedly.
- For example, each color box in the image to the left refers to a group of squares which are almost indistinguishable
- The NL-means filter exploits this property of image self-similarity to eliminate noise
- The squares similar to each other are averaged out.

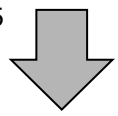
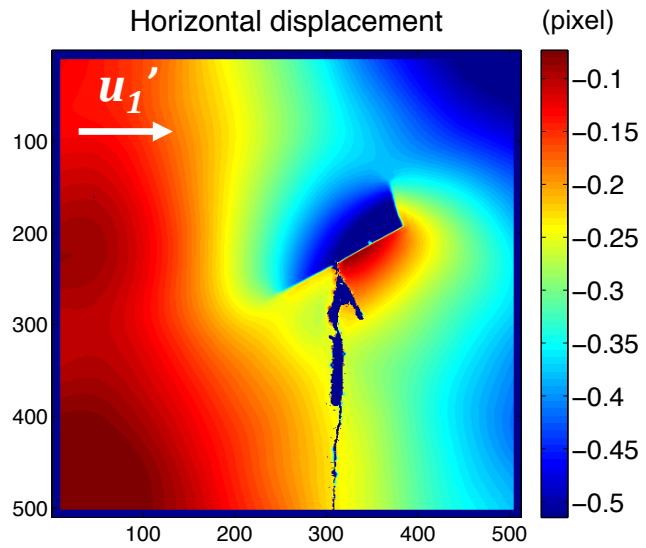
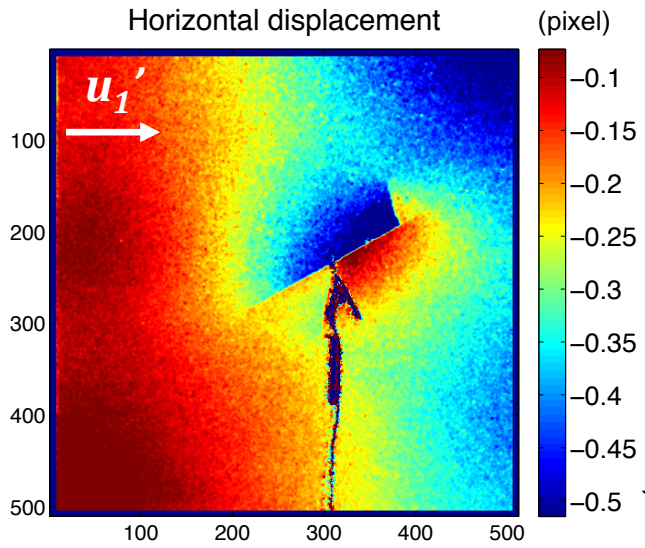
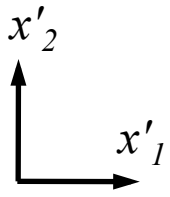


COSI-Corr includes in its tools an implementation of the Non-Local Means algorithm for denoising datasets and images, based on Buades et al., 2008 and Goosens et al., 2008.

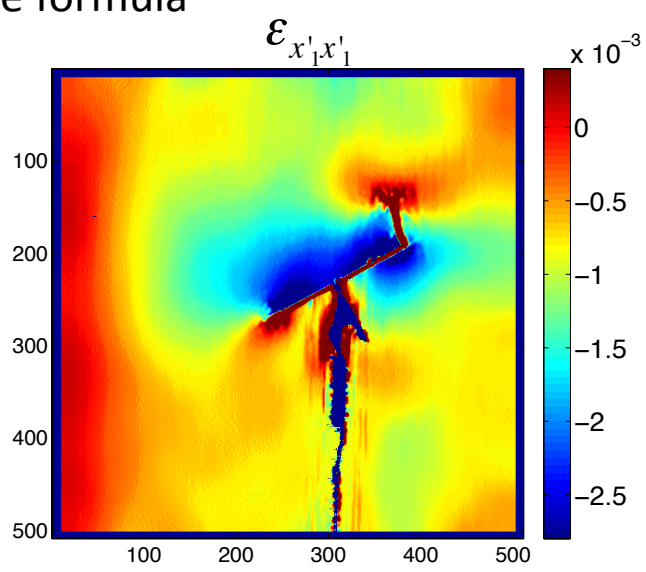
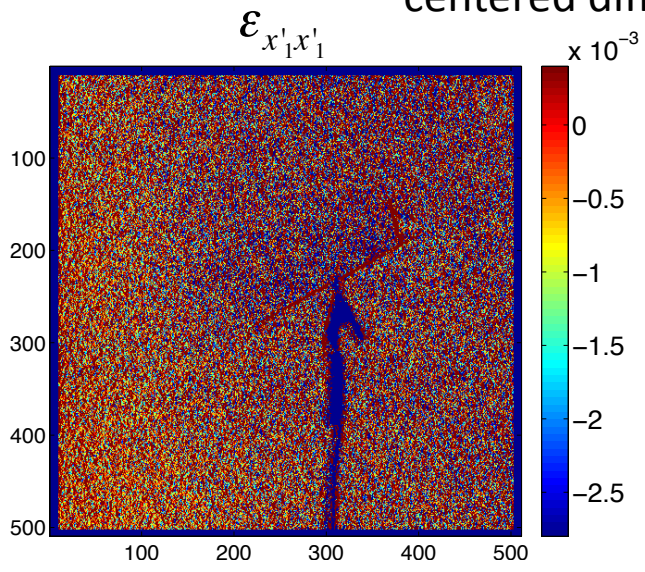
Strain Calculation

Before filtering

After filtering

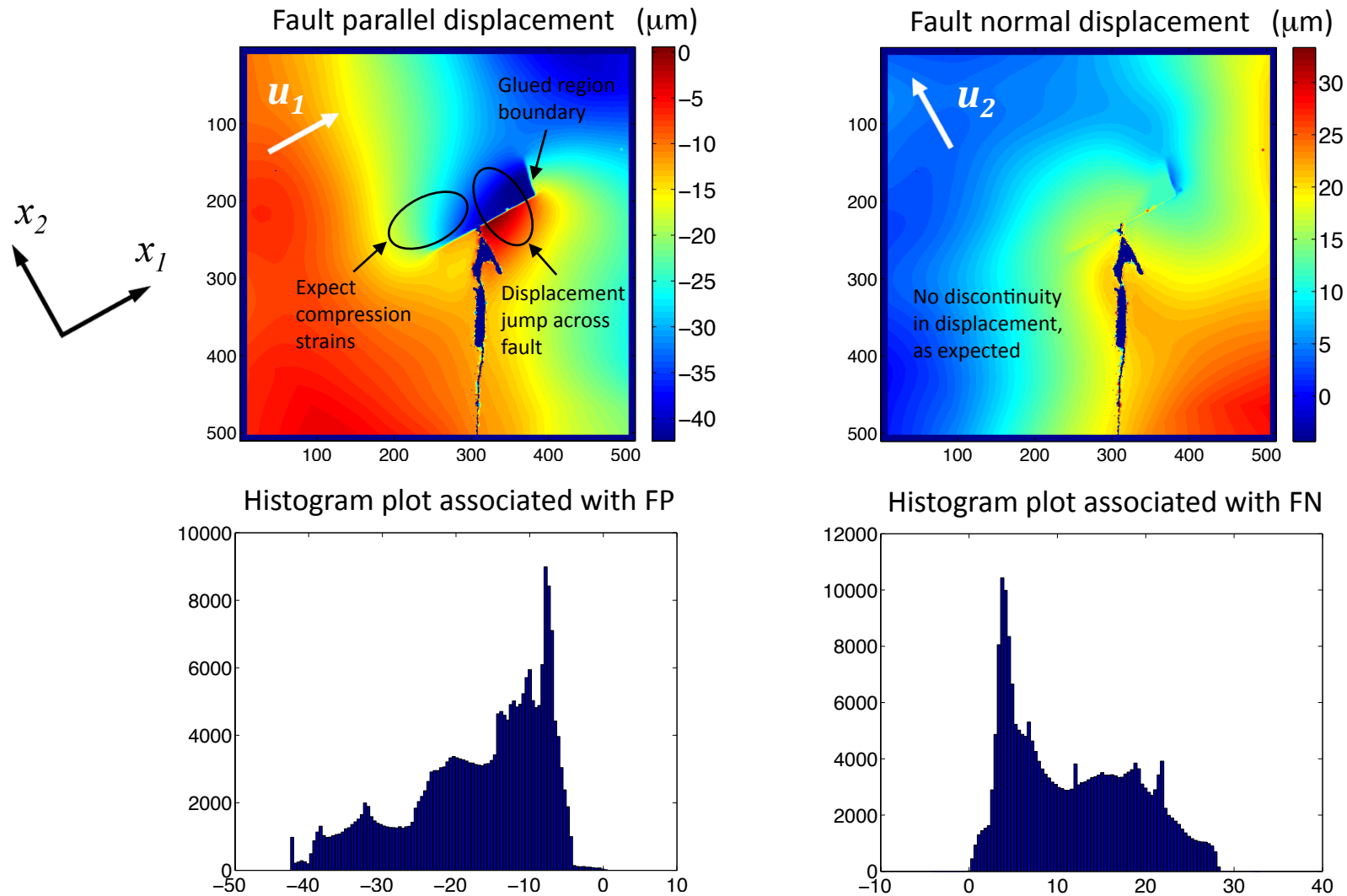


centered difference formula



Fault parallel and fault normal displacements

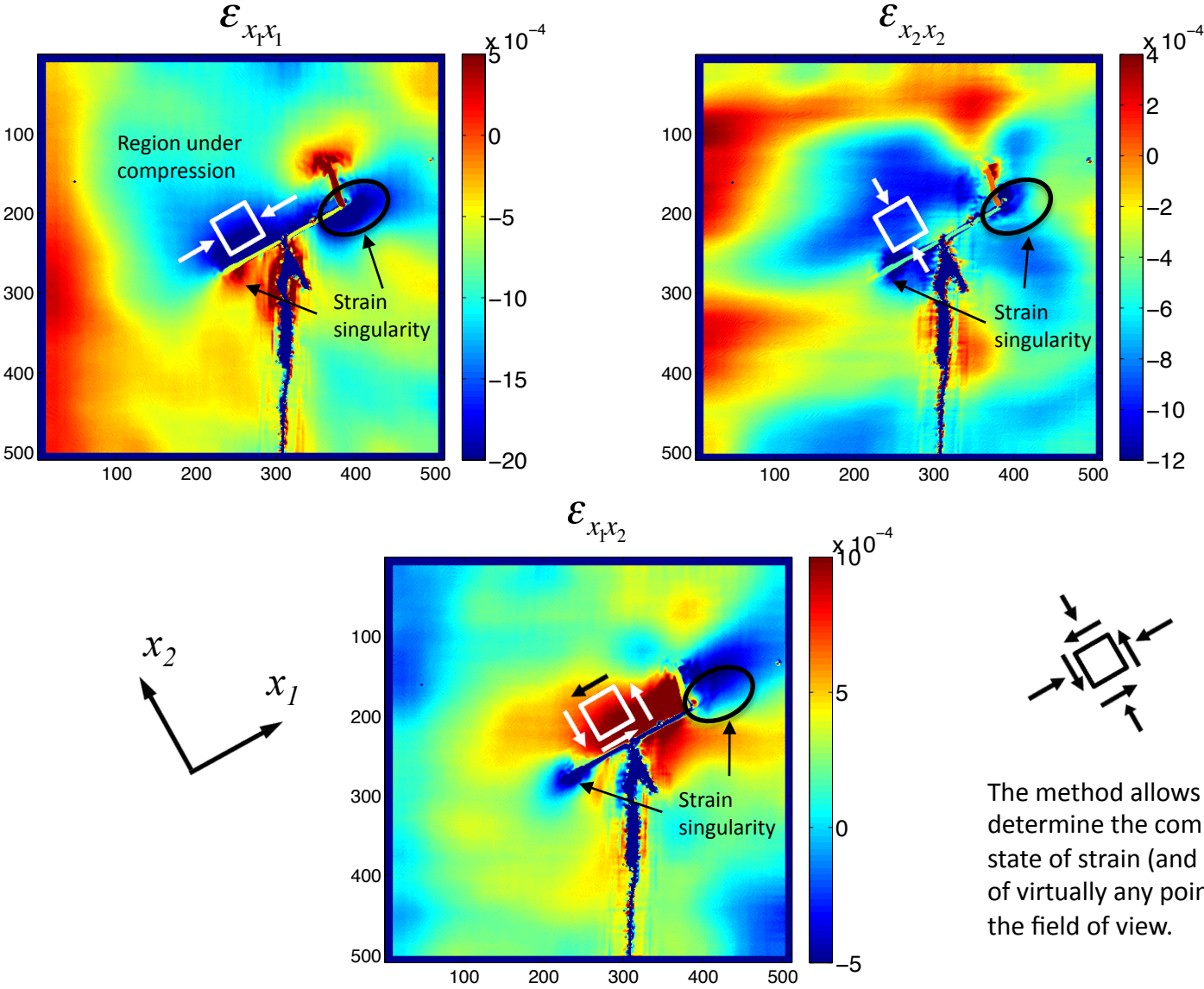
Test 1, $P = 5$ MPa



Overall the results show that rupture has propagated along the frictional interface, consistent with Rosakis et al. (2007), but has been stopped at the glued boundaries.

Normal and Shear Strains

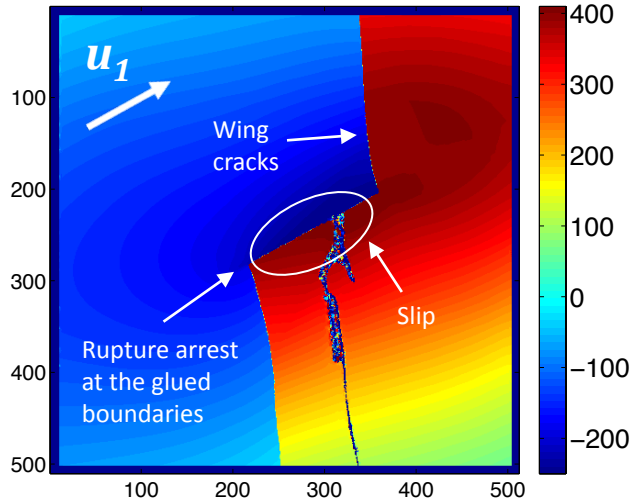
Test 1, $P = 5 \text{ MPa}$



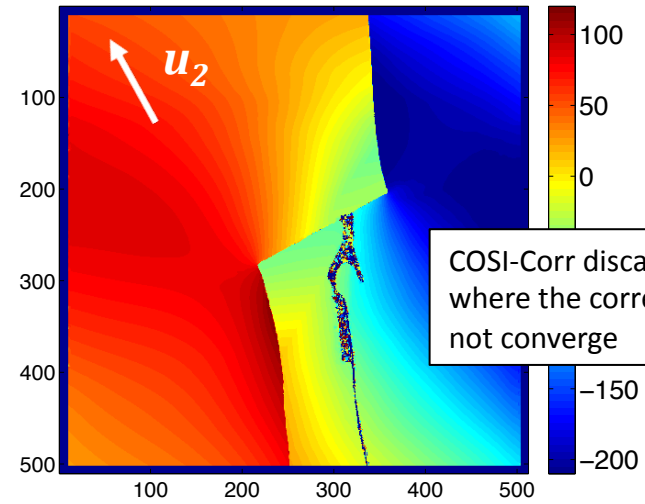
COSI-Corr vs. VIC-2D (Test 2, $P = 15$ MPa)

COSI-Corr

Fault parallel displacement

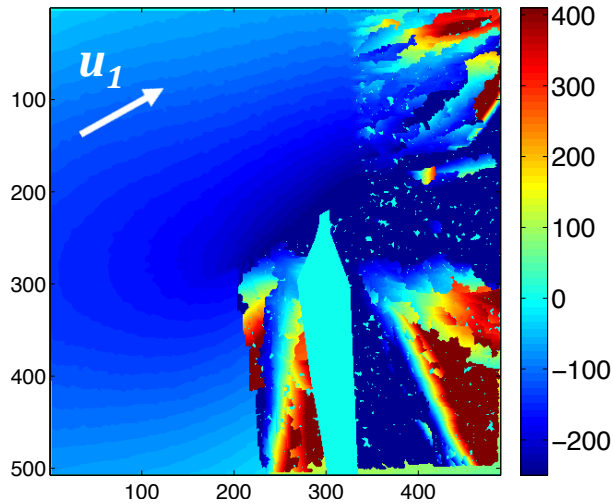


Fault normal displacement

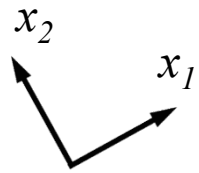
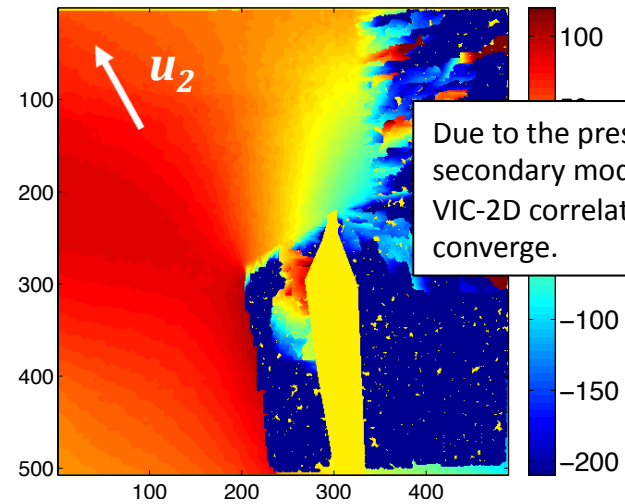


VIC-2D

Fault parallel displacement

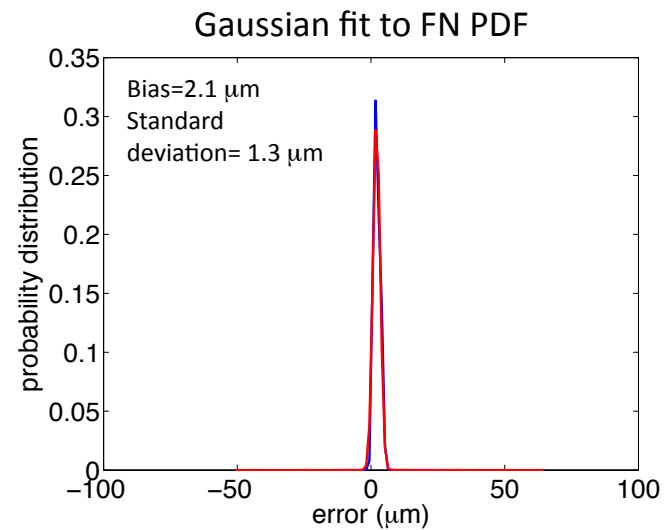
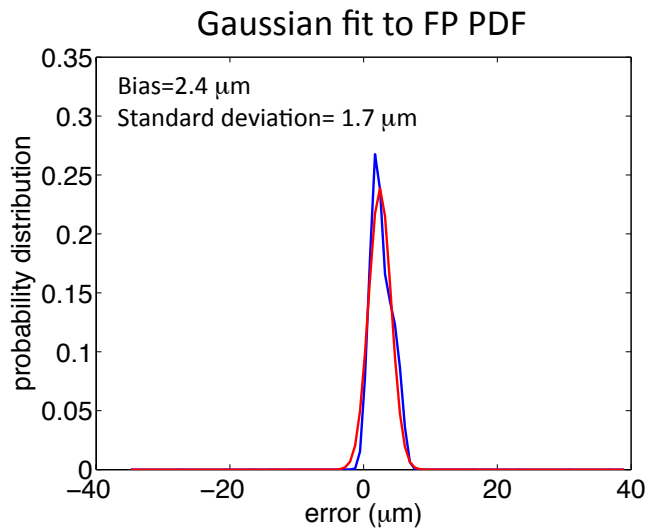
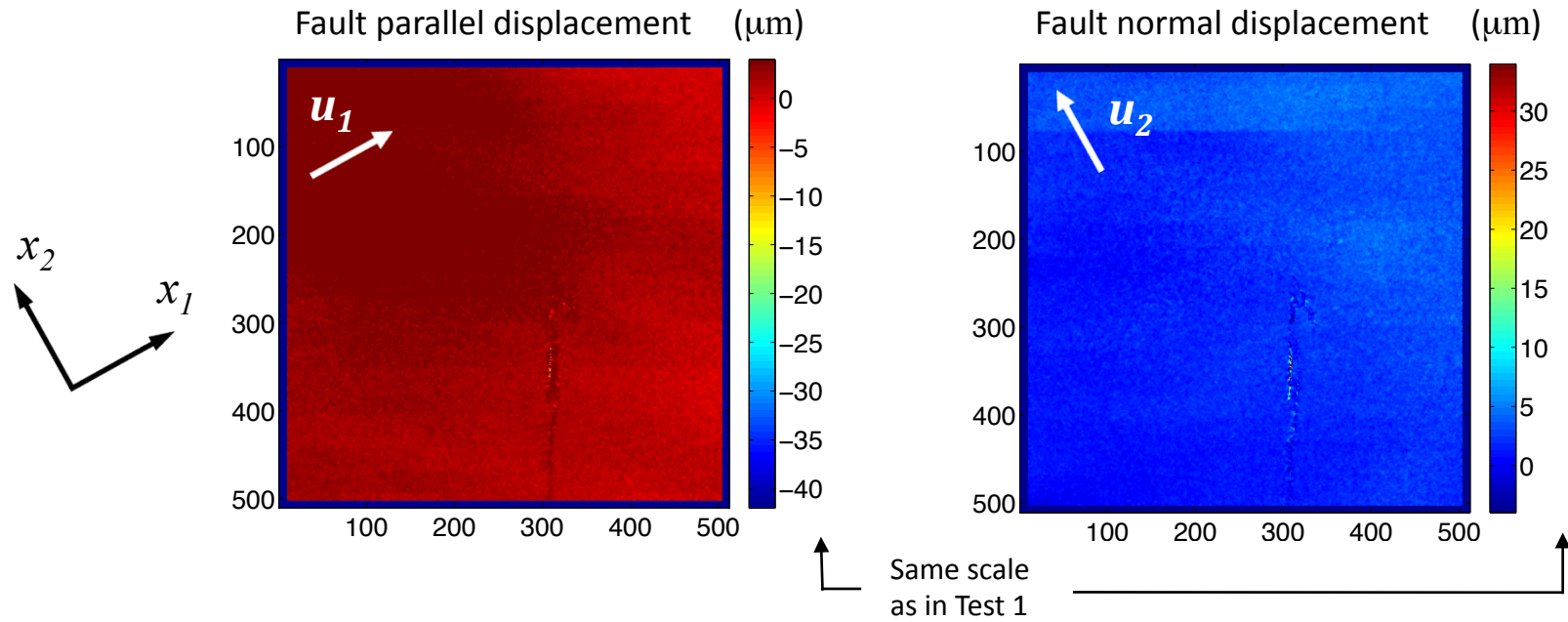


Fault normal displacement

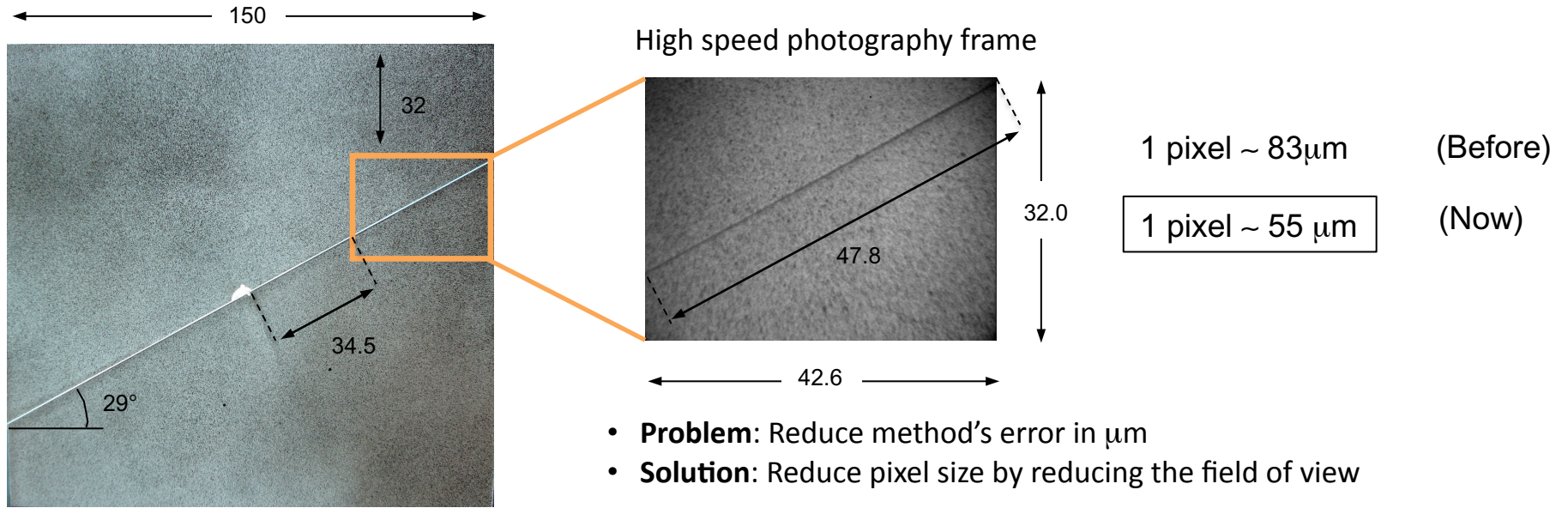


Error Analysis

Correlation of two nominally identical images

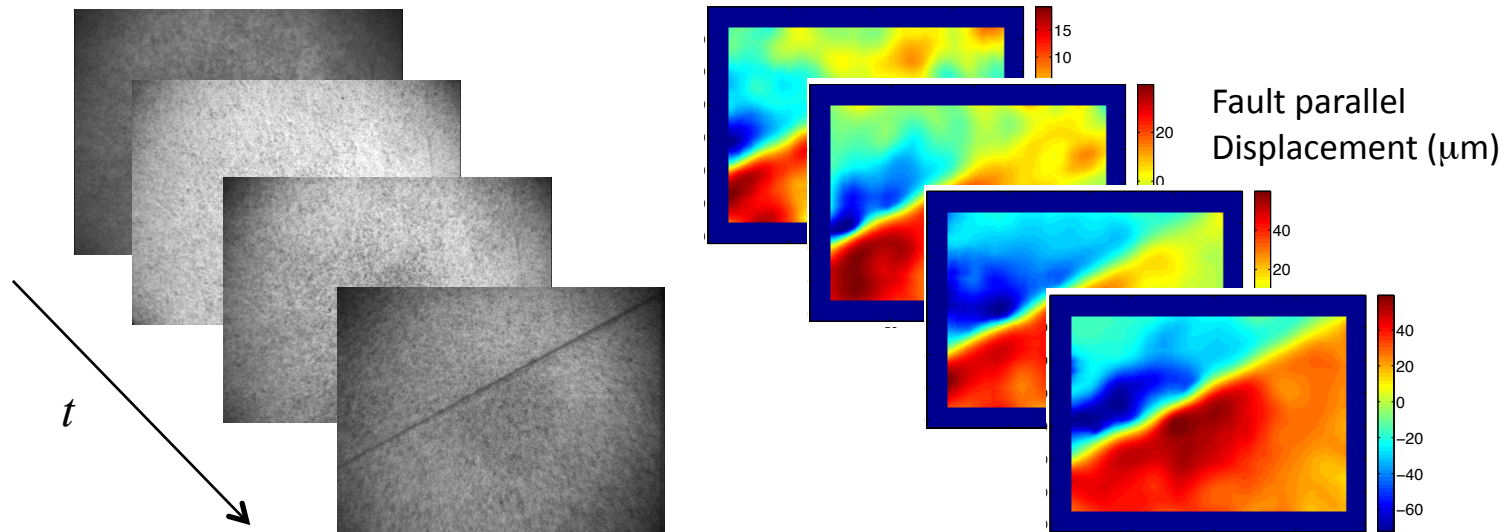


High speed digital image correlation

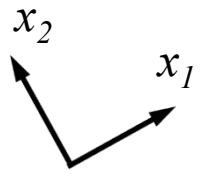


Quotes in mm

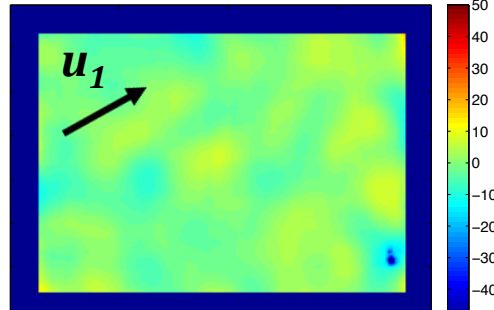
Time-series of displacement fields



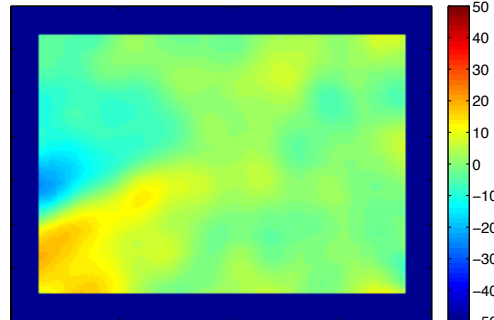
Displacement time series



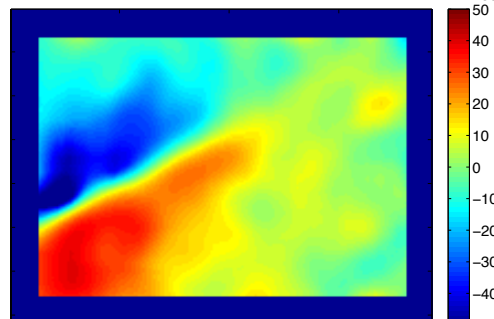
$t = 25 \mu\text{s}$



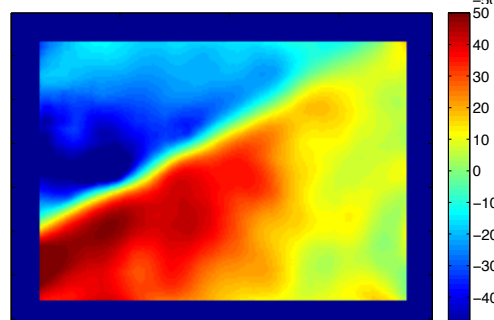
$t = 30 \mu\text{s}$



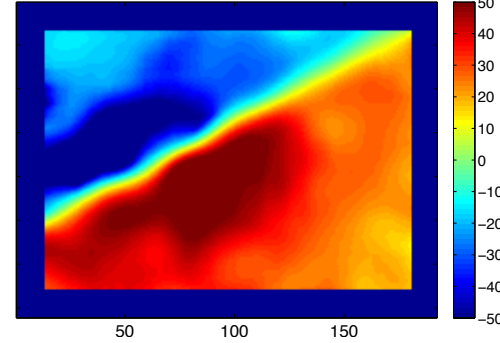
$t = 35 \mu\text{s}$



$t = 40 \mu\text{s}$



Subset: 61 pixels
Step: 4 pixels



NLMeans filter
• Noise par H = 1
• Search area: 21
• Patch size: 5x5

$t = 45 \mu\text{s}$



x_2
 x_1

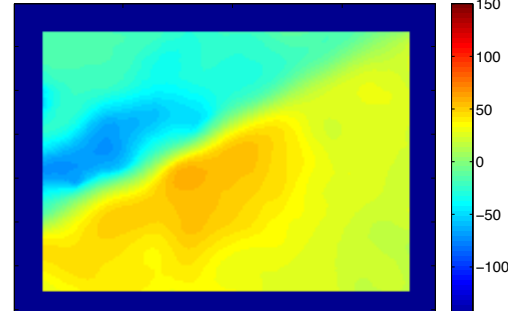
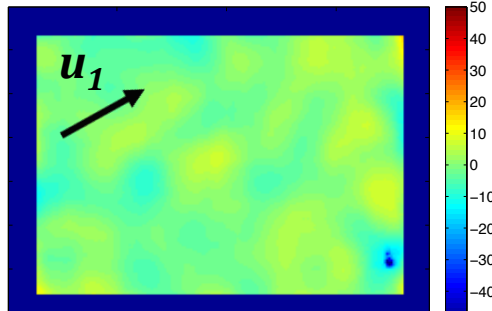
Displacement time series

Subset: 61 pixels
Step: 4 pixels

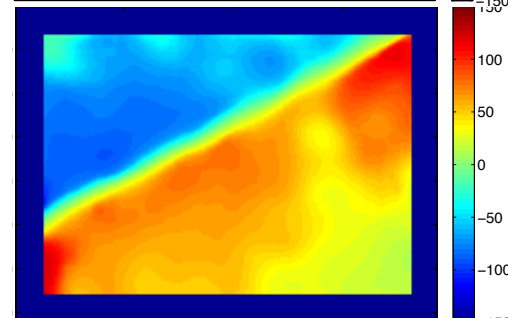
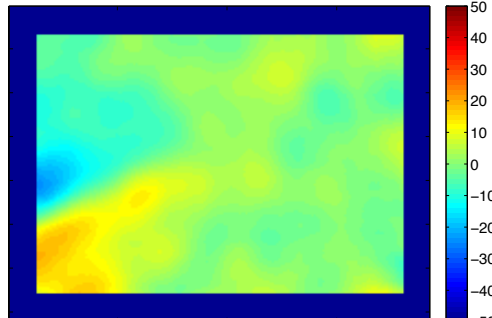


NLMeans filter
• Noise par H = 1
• Search area: 21
• Patch size: 5x5

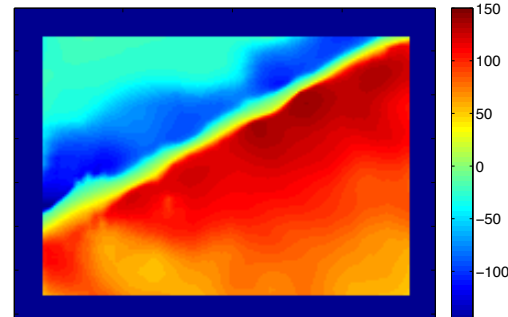
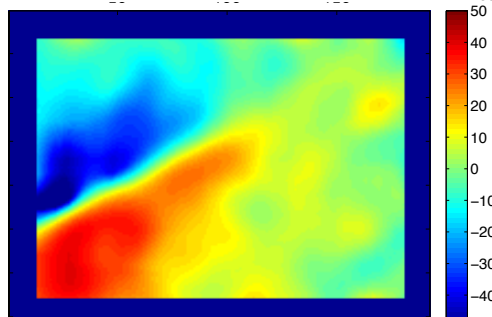
$t = 25 \mu s$



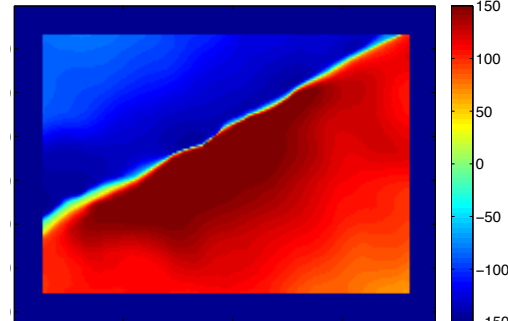
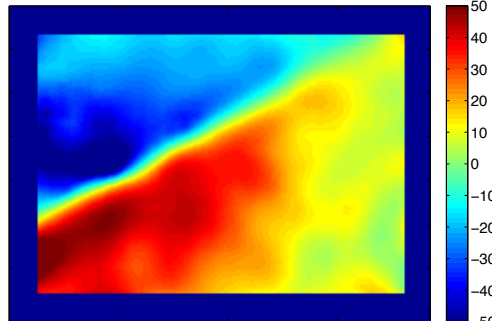
$t = 30 \mu s$



$t = 35 \mu s$



$t = 40 \mu s$



$t = 45 \mu s$

$t = 50 \mu s$

$t = 55 \mu s$

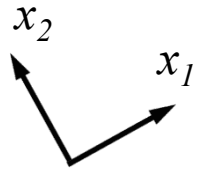
$t = 60 \mu s$

50 100 150

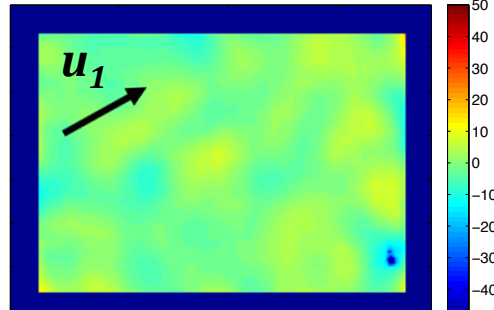
50 100 150



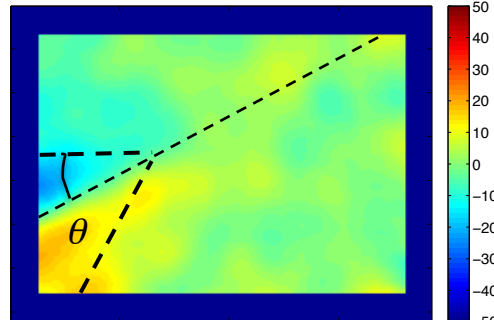
Displacement time series



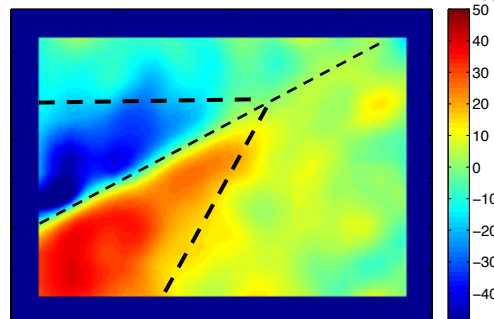
$t = 25 \mu\text{s}$



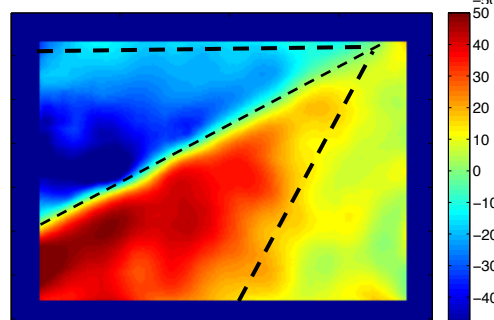
$t = 30 \mu\text{s}$



$t = 35 \mu\text{s}$



$t = 40 \mu\text{s}$

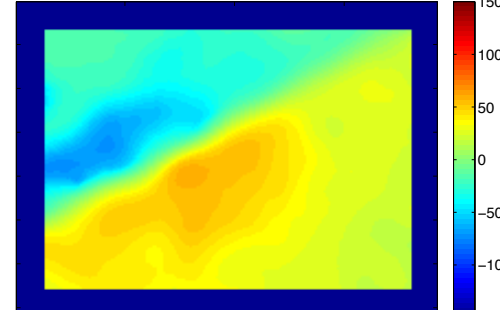


Subset: 61 pixels
Step: 4 pixels

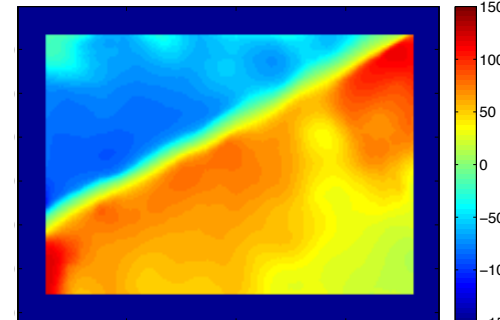


NLMeans filter
 • Noise par H = 1
 • Search area: 21
 • Patch size: 5x5

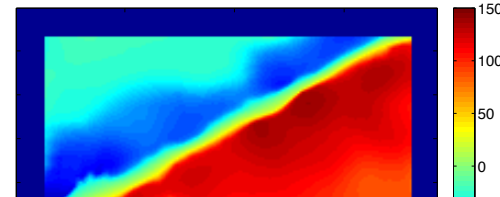
$t = 45 \mu\text{s}$



$t = 50 \mu\text{s}$



$t = 55 \mu\text{s}$



- Interface length (shown in frame): $\sim 40 \text{ mm}$
- Rupture goes through interface in $t < 20 \mu\text{s}$
- Computed rupture speed: $v_r \sim 2.5 \text{ mm}/\mu\text{s}$
- Compare to Homalite wave speeds:
 - $c_s = 1.29 \text{ mm}/\mu\text{s}$
 - $c_p = 2.61 \text{ mm}/\mu\text{s}$
- Mach cone angle is given by:
 $\sin \theta = c_s / v_r, \theta \sim 30^\circ$
- Mach cone will advance $\sim 12.5 \text{ mm}$

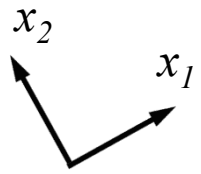


50 100 150

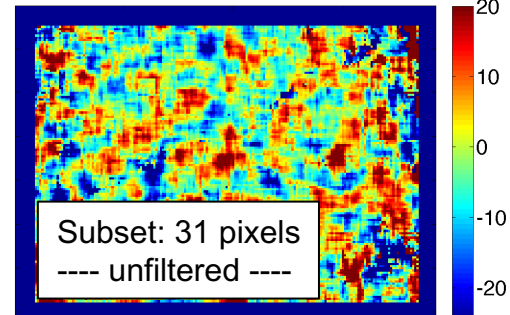
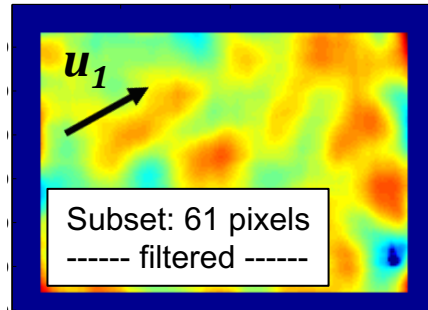
50 100 150

Displacement time series – Fault parallel

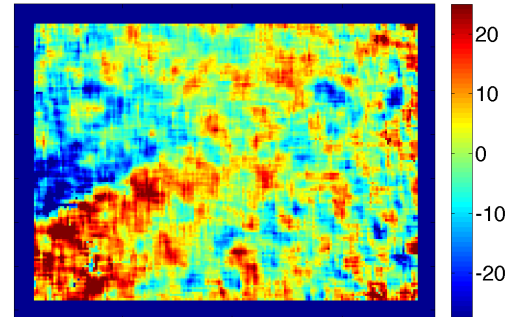
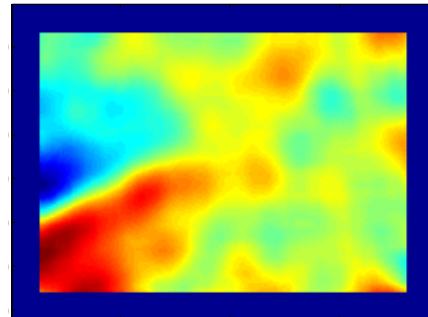
Subset of 61 vs 31 filtered



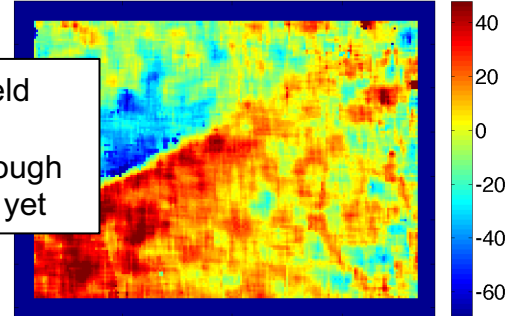
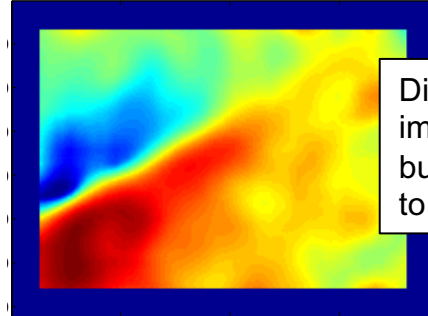
$t = 25 \mu\text{s}$



$t = 30 \mu\text{s}$

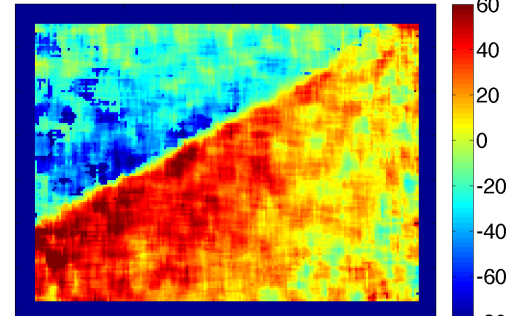
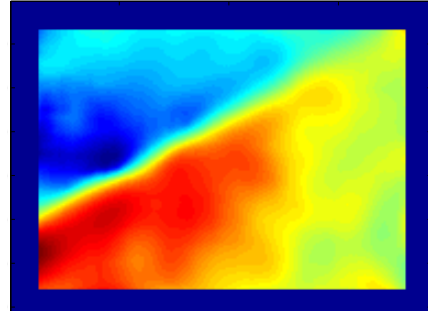


$t = 35 \mu\text{s}$



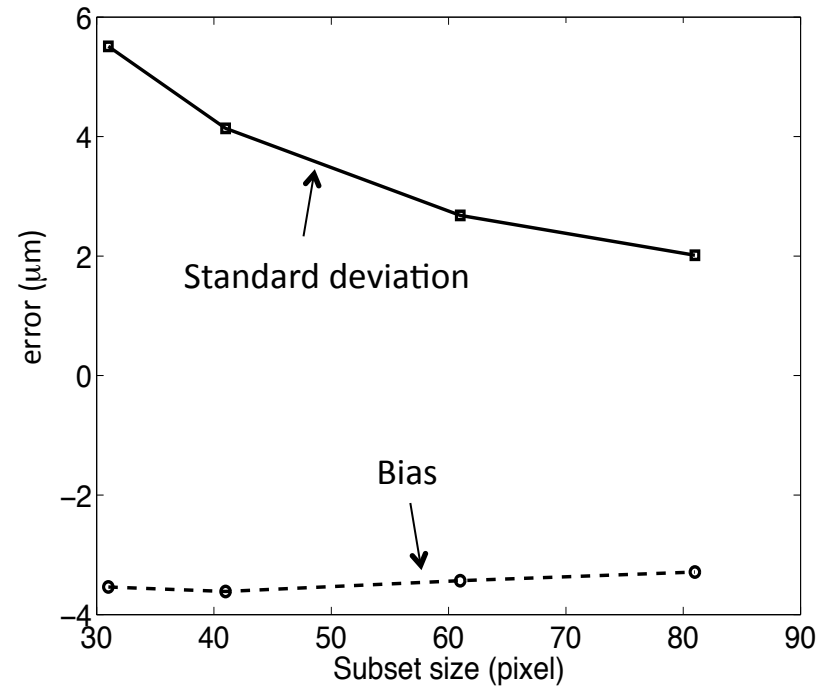
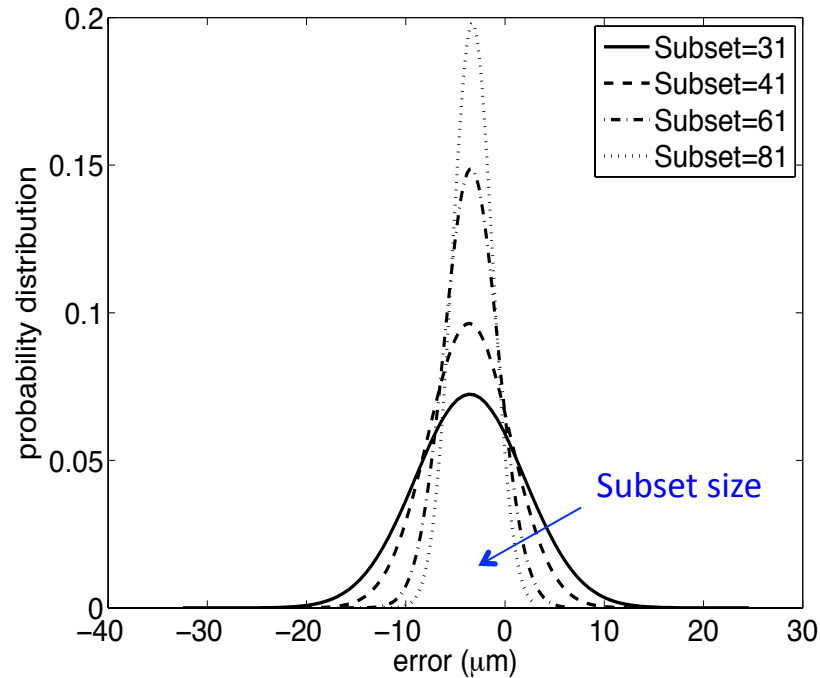
Displacement field improved... but not good enough to obtain strains yet

$t = 40 \mu\text{s}$



Quantifying errors (from gaussian fits)

Effect of subset size

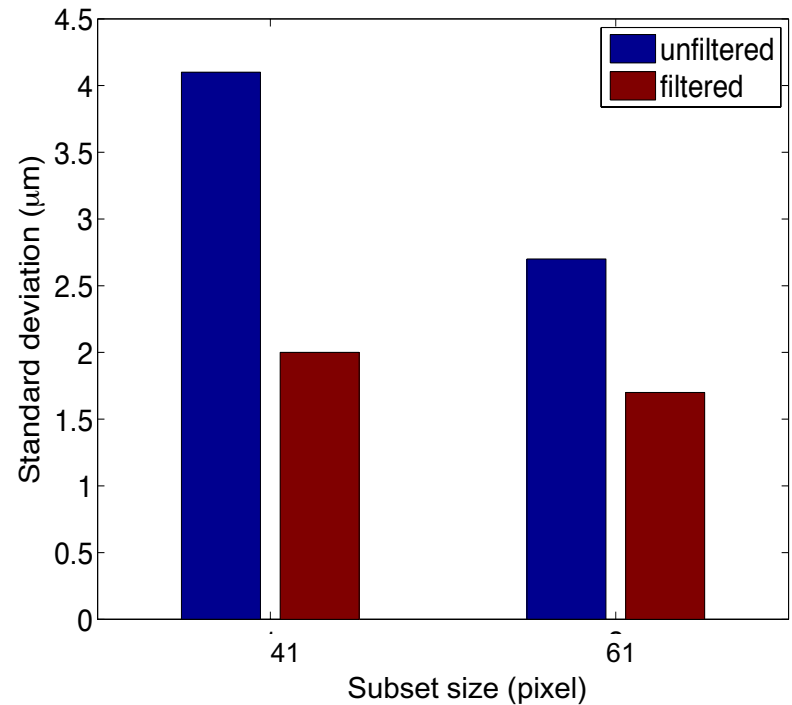
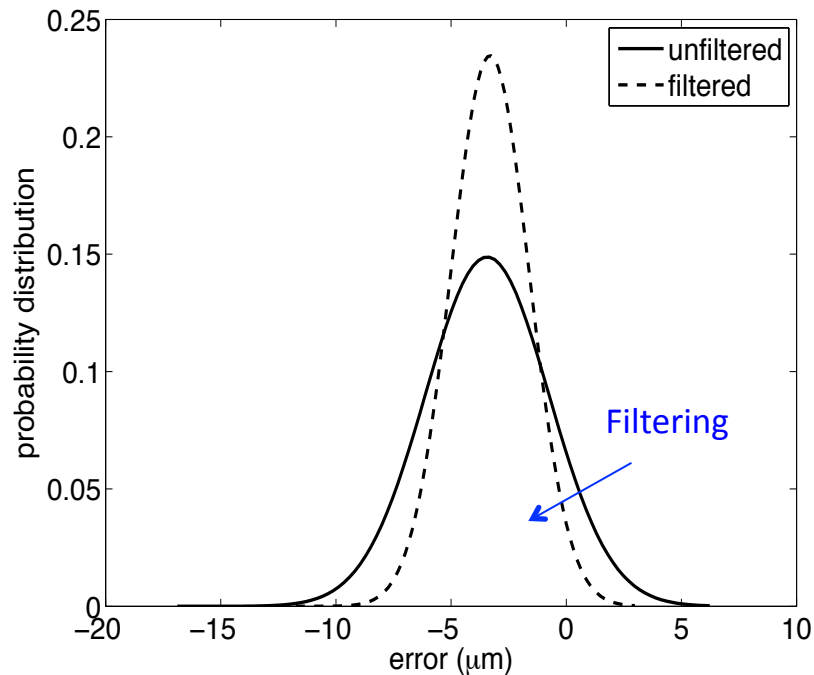


↑ Fault parallel component of displacement, similar results for fault normal ↑

- Correlate two nominally identical images
- The displacement field obtained is taken as a measure of the method's error
- Increasing the subset size has the effect of reducing the error **standard deviation** but not the **bias**

Quantifying errors (from gaussian fits)

Effect of filtering



↑ Fault parallel component of displacement, similar results for fault normal ↑

- Correlate two nominally identical images
- The displacement field obtained is taken as a measure of the method's error
- Filtering with the NLMeans has the effect of reducing the error **standard deviation** but not the **bias**

Standard deviation can be reduced by filtering and increasing subset size, how about the bias?

How can we reduce the bias?

BIAS
due to

- Interpolation
- Noise
- Mismatched shape functions
- Image contamination (e.g. dust on sensor)
- Aliasing -> speckle pattern
- Other causes e.g. lighting change, pattern degradation

Sutton et al., 2009

Static vs. Dynamic Bias

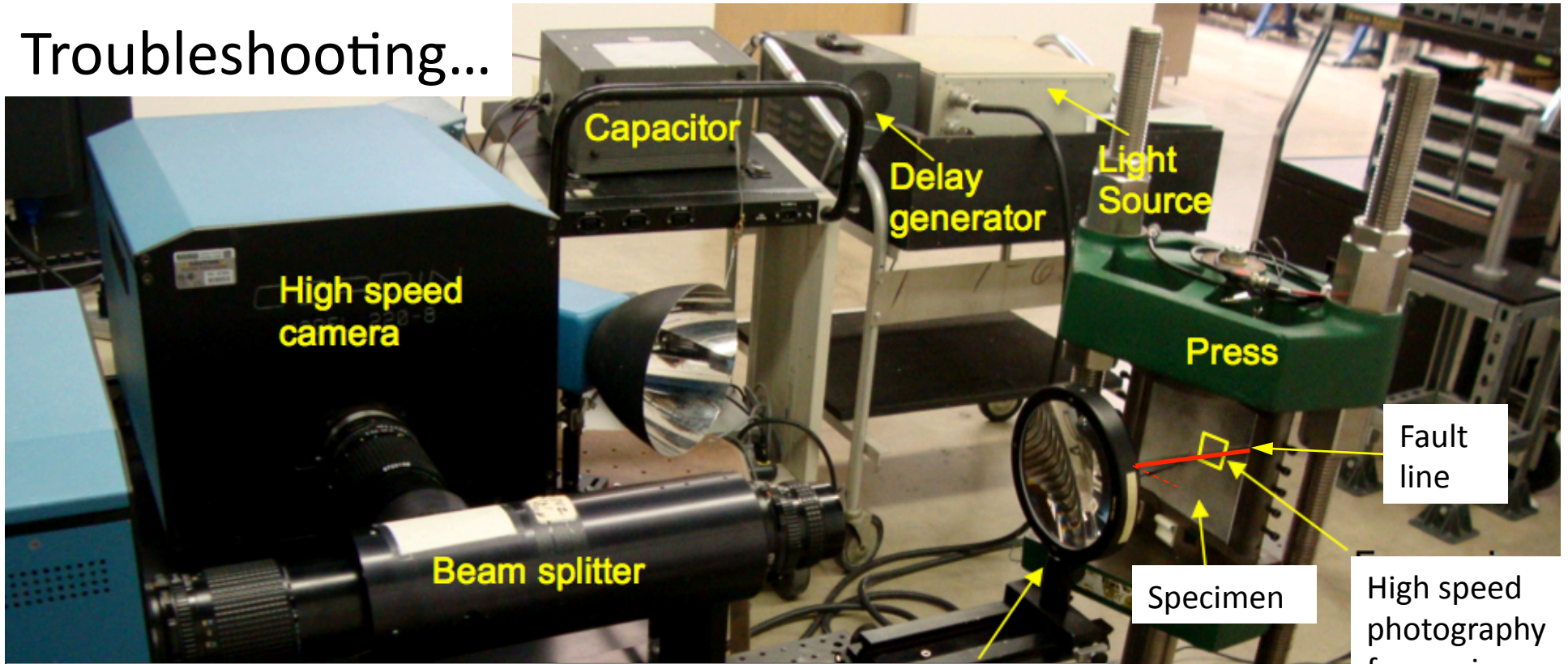
<i>Regime</i>	Static	Dynamic
Pixel size	83 μm	83 μm
Bias (μm)	2.4 μm	3.5 μm
Bias (pixel)	1/35 pixel	1/16 pixel

Dynamic bias is ~ 2.2 times larger than static

$$2.4 \mu\text{m} \times \frac{1}{83} \frac{\text{pixel}}{\mu\text{m}} = 0.0289$$

How can we do better?

Troubleshooting...



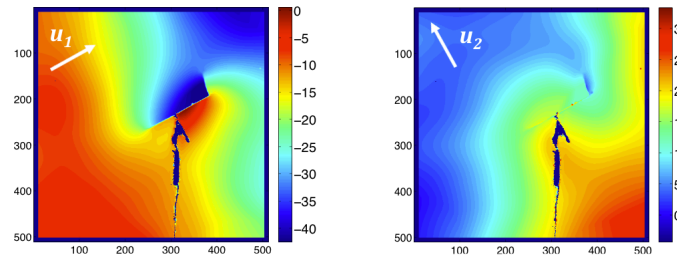
Measurement chain involves:

- **Specimen** → speckle pattern
 - fine (3-4 pixels)
 - coarse (>6 pixels)
- **Plano convex lens** → may introduce distortions
- **Light source** → lighting change from image to image
- **Intensified high speed camera** → will tests two other technologies which
 - may reduce the noise/error but
 - exposure time is worse/larger
- **Correlation algorithm**
 - COSI-Corr** more accurate
 - VIC-2D** more robust to noise

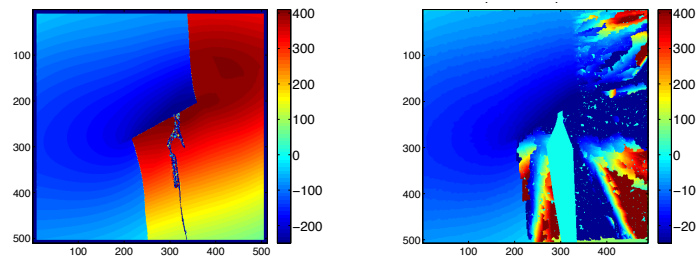


Conclusions and Future Work

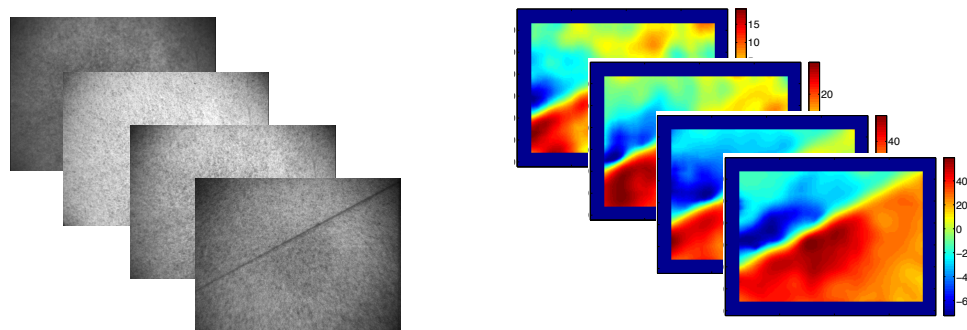
- Successfully characterized full-field static displacements and strain of a dynamic crack with digital image correlation techniques.



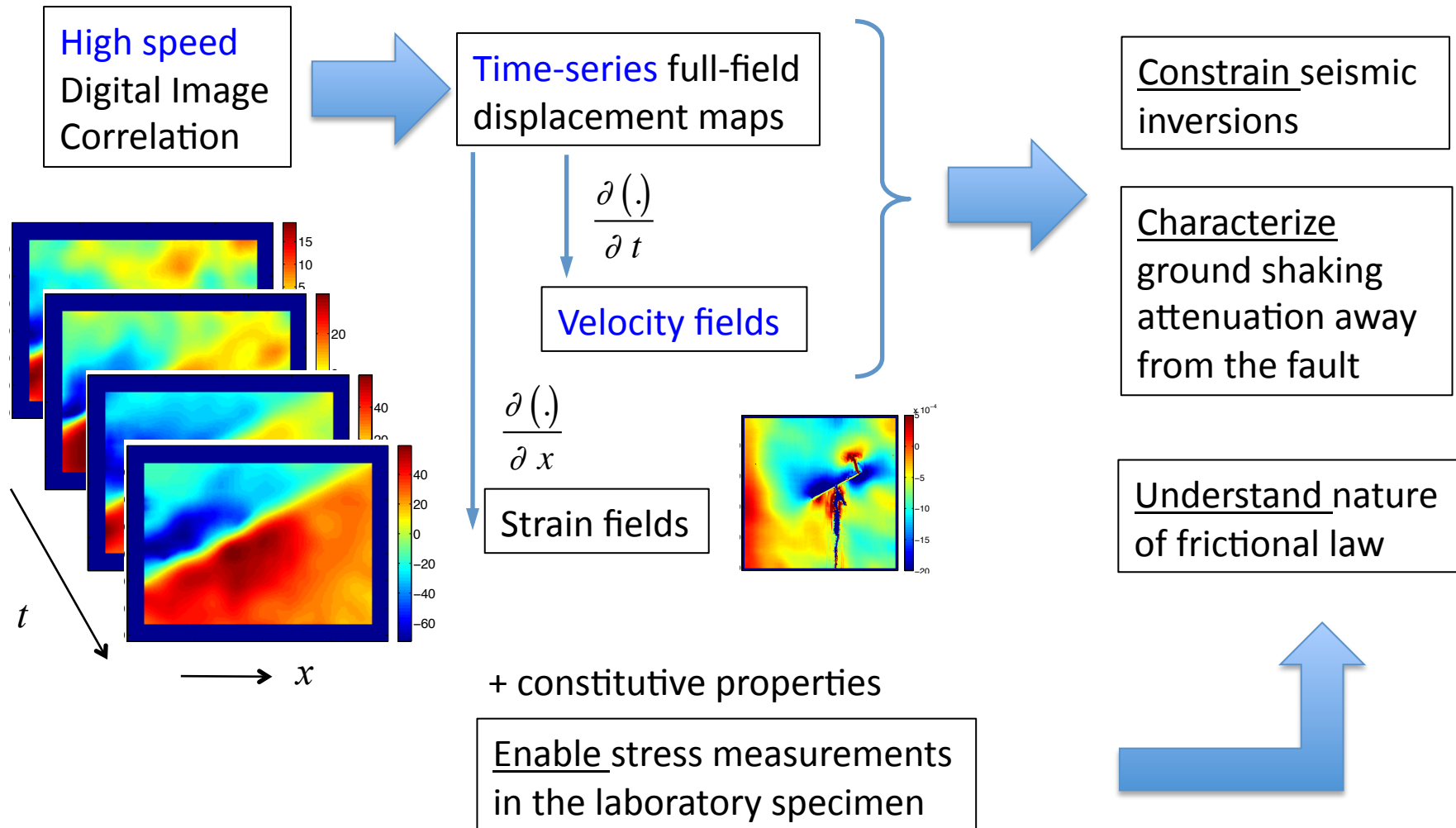
- Two DIC software packages have been tested: COSI-Corr outperforms VIC-2D, especially in the presence of opening cracks, such as in Test 2.



- Performed dynamic measurements with high speed camera to capture the time dependent behavior.



Broader goals of the project



- Study the effects of surface roughness and variability, material inhomogeneity, etc.
- Include spontaneous nucleation