The Effect of Asymmetric Damage on Dynamic Shear Rupture Propagation I: No Mismatch inBulk Elasticity

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Abstract. High-speed digital photography was used to study rupture propagation on the interface between transparent damaged and undamaged photoelastic plates. Bilateral ruptures were nucleated on pre-machined faults at an angle $\alpha$ to the uniaxial loading axis. Stress concentration at the crack tips produced fringes in polarized laser light that allowed their positions to be measured in successive photos. We found that fracture damage introduces a strong asymmetry in propagation speed different from that expected due to the lower elastic stiffness in the damaged material alone. When the tensile lobe of a rupture tip propagated through the damaged material the velocity of that rupture was reduced or stopped. By contrast, when the compressive lobe of a rupture tip passed through the damage, the velocity of that rupture was unaffected by the damage. A physical interpretation is that passage of a tensile lobe through the damage expends energy by lowering the normal stress on pre-existing cracks thus allowing frictional sliding along the crack surfaces. When the compressive lobe of the rupture passes through the damage, compressive stresses prevent sliding, only minor energy is dissipated, and the damage has almost no effect on the velocity. This effect can produce asymmetric propagation for earthquake ruptures on slip surfaces near the edge of a highly damaged fault zone.

1. Introduction

Large displacement faults often juxtapose rocks with different elastic stiffness across the fault plane. Experimental and theoretical studies on such elastic bimaterial interfaces have found that propagation is asymmetric (Rosakis et al. [2007] and references therein). A rupture propagating in the direction of motion of the more compliant material (termed the positive ‘+’ direction) travels with a different speed than a rupture propagating in the opposite negative ‘−’ direction. Numerical studies have shown that this asymmetric propagation is caused by a reduction in the normal stress at the tip of ruptures propagating in the ‘+’ direction, thus favoring propagation in this direction [Weertman, 1980; Harris and Day, 1997; Cochard and Rice, 2000; Rice, 2001; Ranjith and Rice, 2001; Ben-Zion, 2001; Xia et al., 2005b; Shi and Ben-Zion, 2006; Rubin and Ampuero, 2007].

Experimental studies of rupture propagation on bimaterial interfaces by Xia et al. [2005b] observed bilateral asymmetric propagation in all cases. Ruptures in the ‘+’ direction propagated at the generalized Rayleigh wave speed while those in the ‘−’ direction transitioned to super-shear speeds approaching $P_{\text{slow}}$, the $P$ wave speed in the slower (more compliant) material. These results are consistent with the seismological observation of asymmetric supershear propagation in the ‘−’ direction during the 1999 Izmit earthquake on the North Anatolian Fault in Turkey [Bouchon et al., 2001; Rosakis et al., 2007].

Field studies suggest that this representation of a fault as a planar contact between two intact elastic wall rocks may be too simple. In real faults, many of which have been examined from seismogenic depths by uplift and erosion, the wall rocks are separated by layers of fragmented rock classified according to grain size as fault breccia, gouge, or cataclasite as in Figure 1 (see Ben-Zion and Sammis [2003] and Biegel and Sammis [2004] and references therein for a more complete review of fault zone structure). For the San Andreas fault, a 100-200 meter wide low velocity zone associated with this fragmented layer has been mapped seismically to depths of 7 km [Li and Malin, 2008]. Seismic velocities have been observed to decrease in the fragmented layer during an earthquake followed by an exponential-like recovery over time suggesting an interaction between the propagating rupture and the fracture damage [Marone et al., 1995; Li and Vidale, 2001; Li et al., 2003].

Theoretical and experimental studies have demonstrated that off-fault damage can reduce rupture speed below that due to the decrease in elastic stiffness alone [Andrews, 2005; Templeton and Rice, 2007; Biegel et al., 2008]. In these studies, the additional slowing appears to be caused by nonlinear dissipation in the stress concentrations at the crack tip. Rice et al. [2005] have shown that the spatial extent of the interaction between the tip of a propagating slip pulse and off-fault damage is approximately the same as the distance behind the crack tip over which friction decreases from its static to its lower dynamic value, commonly termed $R_o$. By fitting the slip distributions measured by Heaton [1990] for seven large earthquakes, they found that $R_o$ ranged from meters to tens of meters at the centroid depths of the earthquakes (typically between 5 and 15 km). In contrast $R_o$ for Homalite is of the order of 1 cm for our loading conditions.

The question we wish to address here is whether the fault zone damaged layer can produce additional asymmetric
propagation beyond that caused by a contrast in undamaged wall rock stiffness across the fault plane? If the earthquake rupture propagates on a localized surface down the center of the damaged layer, then symmetry precludes this scenario. However, if slip is localized at or near the boundary between a damaged layer and the wall rock, then it is possible that the lower velocity in the damaged layer, or anelastic dissipation in the fragmented rock, or both may produce additional asymmetry in the propagation. The demonstration by Rice et al. [2005] that the spatial scale of interaction is the same order as the spatial extent of the damaged layer suggest that such asymmetry may be possible.

In this paper we use high-speed digital photography to study the propagation of ruptures on the interface between damaged and undamaged photoelastic Homalite plates in the laboratory. We find that fracture damage introduces a strong propagation asymmetry beyond that expected due to the lower elastic stiffness in the damaged material.

2. Experimental Apparatus and Procedures

We use the same apparatus and follow the same procedures described by Xia et al. [2004], Xia et al. [2005b], Rosakis et al. [2007], Lu et al. [2007] and Biegel et al. [2008]. Square plates of the transparent photoelastic polymer Homalite (15.25 cm x 15.25 cm x 1 cm) were bisected by a saw-cut fault at an angle $\alpha$ to one edge. The contacting faces were lapped with #220 sandpaper. Mean surface roughness was measured to be about 2 mm using a digital contact profilometer. As shown in Figure 2, the samples were loaded with uniaxial stress $P$ and a dynamic fracture was nucleated by using a high voltage pulse to explode a wire across the center of the fault plane. The explosion reduced normal stress on a patch of the fault approximately 1 cm long thereby nucleating a rupture which, in most cases, propagated bilaterally. The voltage pulse also triggered high-speed digital cameras which take a series of pictures of the propagating rupture using transmitted polarized light that resolved the photoelastic fringes produced by the spatial gradients in shear stress (Figure 3). The experiments described here differ from those in previous studies in that the half-plate below the fault was fracture damaged as shown in Figure 3. Fracture damage was generated as described in Biegel et al. [2008] by using a razor knife to produce a grid of scratches approximately 2 mm apart oriented at $\pm 45^\circ$ to the loading axis, and then dipping the plate in liquid nitrogen for about 45 seconds.

3. Elastic Properties of Damaged Homalite

The elastic properties of undamaged and damaged Homalite are summarized in Table 1. The shear speed in damaged Homalite was measured in the dynamic rupture experiments by Biegel et al. [2008]. The observed decrease in shear speed corresponds to a fracture density parameter near $\epsilon = 0.2$ in the O’Connell and Budiansky [1974] model. For this value of $\epsilon$, their model predicts a 20% reduction in P wave speed $V_p^0$ and a 17% reduction in Poisson’s ratio $\nu$, as in Table 1. The value of $\epsilon = 0.2$ was calculated from the observed reduction in $c_s$ with the value calculated using its definition $\epsilon = N (a^{-3})$ in terms of the observed volume density $N_V = 1.1$ cm$^{-3}$ and average radius $a = 0.6$ cm of the fractures found using standard stereology (see Biegel et al. [2008]).

An important parameter used to describe mode II rupture propagation on the interface between two elastic materials with different moduli is the generalized Rayleigh speed which is found by solving the following equation Rice [2001]:

$$f(V) = \left(1 - b_1^2\right) a_1 G_2 D_2 + \left(1 - b_2^2\right) a_2 G_1 D_1 = 0$$  (1)

where $a_n = \sqrt{1 - (V/c_n)^2}$, $b_n = \sqrt{1 - (V/c_n)^2}$ and $D_n = 4a_n b_n - \left(1 - b_n^2\right)$. In these expressions, $V$ is the rupture speed, $G_n$ are the rigidity of the two materials ($n = 1, 2$). Using the elastic properties in Table 1, this equation gives $c_{GR} = 906$ m/s for an interface between damaged and undamaged Homalite.

4. Measurement of Rupture Velocity and Supershear Transition Length

We measured the crack tip position as a function of time from the isochromatic fringe patterns in successive high-speed digital images. These data were then fit with either an interpolating cubic spline or a smoothing spline using the curve fitting toolbox in MATLAB$^{15}$. The resulting fit was then differentiated to obtain instantaneous rupture velocity as a function of time. Rupture velocities in the supershear regime were checked by measuring the Mach angle, $\beta$, in the photographs and using the relationship $c_t/c_s = \text{esc} \beta$. Once rupture velocity was determined as a function of time, the data were interpolated to obtain the exact time at which the rupture speed reached $c_s$, the shear wave speed in Homalite. This time was then used to obtain the corresponding distance at which the supershear transition took place by interpolating the rupture position as a function of time. The transition length was determined for both the left and right crack tips, $L^L$ and $L^R$ respectively. This analysis was done for velocities obtained using both spline fits. Where they differed, the one that gave an interpolated transition length that was most consistent with the first appearance of a Mach cone in the photos was chosen. In cases where the rupture had already transitioned to supershear speed by the time the first photograph was taken, we estimated the transition length using the geometrical relationship given by Rosakis et al. [2007] (see section 4.06.3.2 of that paper).

5. Dynamic Shear Rupture Propagation On A Homalite/Homalite Interface

We begin with rupture experiments in undamaged Homalite for comparison with Xia et al. [2004] and for comparison with ruptures on the interface between damage and undamaged Homalite presented in a later section. Two cases are reported here, one at $P = 12$ MPa and one at $P = 15$ MPa (both had a fault angle of $\alpha = 25^\circ$). Results of the 12 MPa case are summarized in Figure 4.

Our observations agree with Xia et al. [2004, 2005a] in that propagation is almost symmetric and both rupture tips transition to supershear speeds. The slight asymmetry in propagation may be due to a corresponding spatial asymmetry in surface roughness of the interface. However our transition lengths are significantly different than those measured by Xia et al. [2004, 2005a], which may reflect a difference in either surface preparation or nucleation strength [Lu et al., 2008]. Nevertheless, as discussed by Rosakis et al. [2007], our transition lengths decrease with increasing load.

In both cases the rupture accelerates toward the P-wave speed of Homalite. The oscillations in rupture velocity may reflect the accuracy to which we can pick the position of the crack tip in the photos. An uncertainty in position of 0.5 mm leads to an uncertainty of about 200 m/s in instantaneous velocity. Oscillations might also be caused by subtle variations in surface roughness along the interface.

For $P = 15$ MPa and $\alpha = 25^\circ$, recent experiments by Lu et al. [2007] show that a crack-like propagation mode is favored over a slip pulse. Crack-like propagation in our experiment is supported by a propagating front in the isochromatics, behind the main supershear rupture front, that propagates at the Rayleigh wave speed.
6. Dynamic Shear Rupture On The Interface Between Homalite and Damaged Homalite

To explore rupture directionality produced by asymmetric off-fault damage, we conducted a series of experiments in which ruptures propagated on the interface between damaged and undamaged Homalite. As illustrated in Figure 5, dynamic symmetry in these experiments is broken in two different ways. First, the contrast in elastic stiffness between damaged and undamaged Homalite introduces the elastic asymmetry described by the ‘+’ and ‘−’ propagation directions as previously discussed by Xia et al. [2005b]. Second, the stress concentration at the rupture tip introduces an anelastic asymmetry based on whether the tensile or compressive lobe of the crack tip stress concentration is on the damaged side of the interface. More anelastic loss is expected at the rupture tip that propagates in the direction for which its tensile lobe is on the damaged side of the interface, which we term the ‘T’ direction. Less loss is expected in the opposite ‘C’ direction which places the damaged side in compression. The asymmetry arises because local tension relieves normal stress to enhance frictional sliding on the fractures comprising the damage and may even result in local mode I fracture growth. In contrast, local compression increases the normal load which suppressed sliding. These asymmetries are illustrated in Figure 5 which shows that the ruptures propagating to the left are ‘C+’ while those propagating to the right are ‘T’.

Experiments with three different combinations of uniaxial load and fault angle are presented here: P=12 MPa and \( \alpha = 25^\circ \), P=15 MPa and \( \alpha = 25^\circ \), and P=18 MPa and \( \alpha = 28^\circ \). Results for the case P=12 MPa and \( \alpha = 25^\circ \) are given in Figure 6 where it is obvious that rupture propagation is strongly asymmetric. The rupture propagating to the right (in the ‘T’- direction) is suppressed for about 26\( \mu \)s before accelerating to a rupture speed that oscillates around the general Rayleigh wave speed \( c_{GR} \). Rupture propagation to the left (in the ‘C+’ direction) transitions to supershear speed almost immediately upon nucleation and accelerates toward the P-wave speed in undamaged Homalite. This behavior is quite different from that observed by Xia et al. [2004, 2005a] for ruptures on the interface between Homalite and polycarbonate where, for the same P and \( \alpha \), rupture in the ‘+’ direction propagated at \( c_{GR} \) while rupture in the ‘−’ direction propagated at the supershear speed \( P_{slow} \), the P wave speed in the more compliant polycarbonate. Since the contrast in shear wave speed across the fault plane is comparable in both systems (80% for polycarbonate/ Homalite and 83% for damaged Homalite/ Homalite), the very different nature of the observed asymmetry implies that damage plays an important mechanical role beyond just reducing the wave speeds.

We propose the following explanation of these observations. Propagation at \( c_{GR} \) in the ‘+’ direction is the same behavior observed for undamaged Homalite in Figure 4. We hypothesize that compressions at the crack tip immobilizes the flaws comprising the damage and they play no role in dynamic propagation. This hypothesis is supported by the observation in Figure 7 that the Mach angles in Homalite and damaged Homalite are nearly equal. The ratio between the S-wave speed in Homalite and in damage Homalite is related the ratio of the Mach angles as

\[
\frac{c_d}{c_o} = \frac{\sin \beta_d}{\sin \beta_o}
\]

where the superscript ‘d’ refers to damaged Homalite. This ratio is plotted as a function of time in Figure 7. Based on the measured velocities in Table 1, the expected ratio is 0.83. The observed value is closer to 0.9 which supports our hypothesis that the mechanical effects of the damage are suppressed on the compressive side of the rupture.

We hypothesize that the delay in propagation in the ‘T’- direction is caused by a significant lowering of the effective elastic modulus on the damaged side of the interface due to activation of the damage by the tension and the activation of off-fault energy dissipation due to frictional sliding. This lower modulus reduces the stress intensity factor below its critical value for propagation. As the rupture length increases in the ‘C+’ direction, the stress intensity factor at the ‘T’- tip increases as the square root of the length of the rupture until it reaches the critical value and rupture is initiated (at about \( t = 26\mu s \)).

When the applied load is increased to 15 MPa at the same fault angle \( \alpha = 25^\circ \), the rupture on the ‘C+’ side once again initiates and propagates at supershear speed whereas the rupture on the ‘T’- side now propagates slightly below the Rayleigh wave speed of Homalite (Figure 8). The slight reduction in rupture velocity, compared to the previous case, may be due to increased damage activation at the higher applied load. Note that the rupture on the ‘T’- side was not delayed in this case.

In Figure 9 the load was increased to \( P=20 \) MPa and the fault angle to \( \alpha = 28^\circ \). In this case the rupture propagated unilaterally at a supershear speed near \( c_0 \) in the ‘C+’ direction. In order to understand this result, consider the case of uniaxial loading where the ratio of the resolved shear, \( \tau \), to the normal stress (positive in compression), \( \sigma \), acting on the fault depends only on the fault angle and is given by

\[
\frac{\tau}{\sigma} = \frac{\sin 2\alpha}{1 + \cos 2\alpha}
\]

By increasing the fault angle from 25\(^\circ\) to 28\(^\circ\) we have increased \( \tau/\sigma \) and brought the fault closer to failure (\( f_s \approx 0.6 \) for Homalite). By increasing the applied load from 15 to 20 MPa we have increased the off-fault stress levels thereby also increasing the effect of damage in retarding or stopping the rupture in the ‘T’- direction. Thus even though the resolved shear stress was increased on the fault, the increased damage activation completely suppressed rupture in the ‘T’- direction.

7. Summary and Conclusions

We have studied the effect of off-fault damage on dynamic rupture propagation. When a fault separates an intact material from the same material which is fracture damaged, the rupture prefers to propagate in the direction for which the compressive stress lobe is in the damaged material. We denote this direction as ‘C+’. In the opposite direction for which the tensile stress lobe is in the damaged material, ‘T’, the rupture propagation is retarded or completely stopped due to two effects. First, displacement on cracks comprising the damage produce a dynamic reduction in elastic moduli which results in the reduction of stored elastic potential energy available for rupture propagation. Second, off-fault energy dissipation due to frictional sliding and rapid opening of the micro-cracks also reduces energy available for propagation.

The effect of load on peak rupture velocity is summarized in Figure 10. Increasing the applied load exacerbates the negative effect of damage on rupture in the ‘T’- direction which overwhelms the positive effect of an increased shear stress on the fault. Propagation in the ‘C+’ direction is nearly the same for damaged and undamaged Homalite which supports our hypothesis that compression in the ‘C’ direction suppresses motion on the damage cracks.

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Table 1. Material properties of sample materials.

<table>
<thead>
<tr>
<th>Material</th>
<th>$c_p$ (m/s)</th>
<th>$c_s$ (m/s)</th>
<th>$\nu$</th>
<th>$\epsilon$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Homalite</td>
<td>2408$^{(1)}$</td>
<td>1200$^{(1)}$</td>
<td>0.35$^{(1)}$</td>
<td>0</td>
</tr>
<tr>
<td>Damaged Homalite</td>
<td>2000$^{(3)}$</td>
<td>1000$^{(2)}$</td>
<td>0.25$^{(3)}$</td>
<td>0.2</td>
</tr>
</tbody>
</table>

(1) Rosakis et al. [2007] (2) Biegel et al. [2008] (3) O’Connell and Budiansky [1974]

Figure 1. Schematic diagram of a fault zone. Most of the slip is accommodated in the fault core, which is typically a few cm thick and is composed of very fine grained crushed rock called cataclasite. Slip is usually further localized on very narrow slip surfaces within the core. The core is bordered by layers of coarser fragmented rock called gouge or breccia. These layers are usually a few meters thick and appear to be shattered in place with little or no shear strain. The gouge and breccia is bordered by fractured but not granulated wall rock in which the fracture density decreases with distance from the fault zone, falling to the background density over a distance of a few hundred meters. More detail is given in reviews by Ben-Zion and Sammis [2003] and Biegel and Sammis [2004] and references therein.
Figure 2. Sample geometry. Homalite plate bisected by a pre-machined fault at an angle $\alpha$ is loaded in uniaxial compression $P$. Exploding wire reduces normal stress on a fault patch which nucleates a bilateral rupture. For details see Rosakis et al. [2007].
Figure 3. Experimental apparatus used to photograph shear stress fringes in a Homalite sample during dynamic rupture. Inset shows sample in loading frame used to apply uniaxial load $P$. The saw-cut fault separating damaged and undamaged Homalite has a normal vector at an angle $\alpha$ to the load. For details see Rosakis et al. [2007].
Figure 4. Snapshots of isochromatic fringe pattern showing contours of maximum shear stress due to a dynamic shear rupture along a frictional interface between two undamaged Homalited plates for applied load, $P = 12$ MPa and fault angle, $\alpha = 25^\circ$. The rupture undergoes a Burridge-Andrews type supershear transition at $t = 28 \mu s$. Normalized rupture velocity $v_r/c_s$ is plotted as a function of time for the left and right crack tips. Open circles indicate times at which the pictures were taken and the solid curves are the instantaneous rupture velocity found by differentiating cubic spline fits to the measured crack tip positions as discussed in the text. Also shown are the normalized Rayleigh wave speed $c_R/c_s$ and normalized P wave speed $c_p/c_s = 2.08$ (upper boundary of the graph). $L_{rT}$ and $L_{lT}$ are the measured (or extrapolated) supershear transition lengths for the left and right crack tips respectively.
Figure 5. Anelastic asymmetry results from the positions of the compressive and tensile stress concentration lobes of the two crack tips within the damaged Homalite. In the ‘C’ direction, the compressive lobe is in the damage while in the ‘T’ direction the tensile lobe is in the damage. Also shown are the ‘+’ and ‘−’ directions defined by the elastic contrast across the fault. The ‘+’ direction is defined as the direction of motion of the more compliant wall rock (damaged Homalite in this case).
Figure 6. Snapshots of isochromatic fringe pattern showing contours of maximum shear stress due to a dynamic shear rupture along a frictional interface separating Homalite and damaged Homalite for an applied load $P = 12$ MPa and a fault angle $\alpha = 25^\circ$. Normalized rupture velocity $v_r/c_s$ is plotted as a function of time for the left and right crack tips. Open circles indicate times at which the pictures were taken and the solid curves are the instantaneous rupture velocity found by differentiating cubic spline fits to the measured crack tip positions as discussed in the text. Also shown are the normalized generalized Rayleigh wave speed $c_R/c_s$ and normalized $P$ wave speed $c_p/c_s = 2.08$ (upper boundary of the graph). $L_T$ is the measured (or extrapolated) supershear transition length for the left crack tip. All velocities are normalized to $c_s$, the shear wave speed in undamaged Homalite.
Figure 7. Comparison of Mach angles $\beta$ in Homalite and $\beta^d$ in damaged Homalite. Upper panel shows the frame at 32 $\mu$s from Figure 7. The lower panel shows the ratio of shear velocities in the damaged and undamaged Homalite. $c^d_s$ is the expected value of the ratio for shear wave speeds in damaged and undamaged Homalite from Table 1. A complete deactivation of the damage by compression would give 1.0.
Figure 8. Same as Figure 6 except the applied load, $P = 15$ MPa.
Figure 9. Same as Figure 6 except the applied load is $P = 20$ MPa and the fault angle is $\alpha = 28^\circ$. 

$P = 20$ MPa  
$\alpha = 28^\circ$

Left Tip (C+)  
Right Tip (T-)  
$L_T = 20$ mm
Figure 10. The effect of load on maximum rupture velocity of a dynamic shear rupture on the interface between Homalite and damaged Homalite. Velocities are also shown at the same pressures for rupture on the interface between two undamaged Homalite plates for comparison. All velocities are scaled to $c_s$, the shear wave speed in undamaged Homalite.